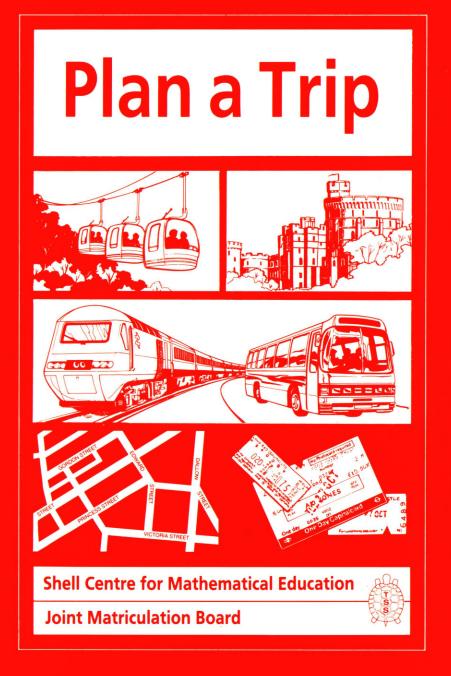
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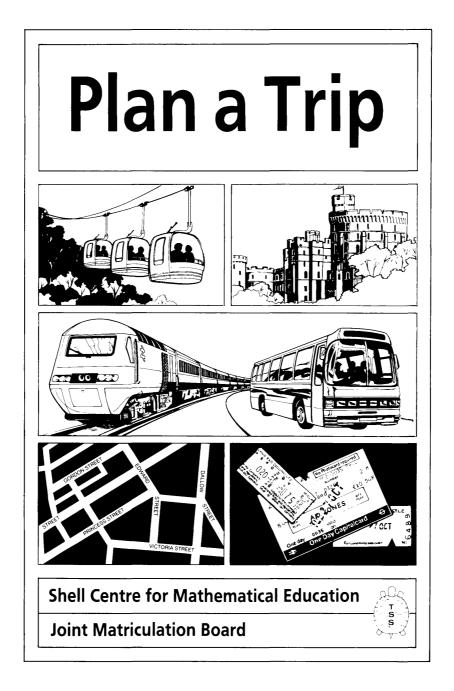


TEACHER'S GUIDE

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TEACHER'S GUIDE

About this scheme . . .

This scheme for the teaching, learning and assessment of numeracy through problem solving consists of a series of modules which provide effective support for teachers of mathematics who wish to introduce into the curriculum a component which enables their students to link their mathematics to the real world in which they live.

It has been developed with students of all abilities in the age range 13–16, and their teachers.

Each module package provides comprehensive materials for both teaching and assessment, related to a practical context which has proved interesting and enjoyable to the students who have taken part in its development. It is accessible to those who normally find mathematics difficult, while at the same time it provides a challenge for the most able.

A Scheme of Assessment based on these modules is offered by the Joint Matriculation Board. It includes both coursework and examination components of the kind illustrated in this book. Successful candidates receive a Statement of Achievement on each module at Basic, Standard or Extension level and, subject to certain conditions, the JMB Certificate of Numeracy through Problem Solving.

The Scheme relates to the GCSE National Criteria in Mathematics.

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Authors

This series of module packages has been developed, as part of a joint project on the assessment of numeracy by the Shell Centre and the Joint Matriculation Board. Many teachers and their students have worked with the central team: Alan Bell, Hugh Burkhardt, Rosemary Fraser, Kevin Mansell, Jim Ridgway and Malcolm Swan together with Barbara Binns and John Gillespie who, assisted by Clare Trott, coordinated the project. Building on previous discussions involving the Shell Centre and the JMB, it was conceived and directed as part of the Testing Strategic Skills programme, by

Hugh Burkhardt

This module, Plan a Trip, has been written by

Malcolm Swan, Barbara Binns and John Gillespie

It is a result of successive revision through five versions on evidence collected from the comments and suggestions of the teachers and students involved, and through classroom observation by the team.

The assessment tasks owe much to the advice of John Pitts.

Many contributions to the work of the project have been made by staff and committee members of the Joint Matriculation Board – notably John Mathews, the Chairman of the JMB's Steering Committee and Austin Fearnley, who has played a major role in the organisation of the operational trials.

Among the teachers and others to whom we are particularly indebted for the contributions to the early development of the module are Roger Brown, David Cain, Joanne Cooper, Rita Crust, Paul Davison, John Edwards, Mick Fitzgerald, Tansy Hardy, Aidan Harrington, Anne Haworth, Steve Maddern, Sue Marshall, Dorothy Martin, Cath Mottram, Mary Robinson, Norbert Gajda, Bob Smith, Aileen Steven, Glenda Taylor, Margaret Tuck, Trish Tunstall and Dave Wilson.

The later trials involved teachers and students in over 50 schools in many local authorities including Barnsley, Bradford, Bury, Calderdale, Cheshire, Cumbria, Derbyshire, Doncaster, Gateshead, Humberside, Kirklees, Knowsley, Lancashire, Leeds, Leicestershire, Manchester, Newcastle upon Tyne, Northumberland, North Tyneside, North Yorkshire, Nottinghamshire, Rochdale, Rotherham, Salford, Sheffield, Stockport, Sunderland, Tameside, Trafford, Wakefield and Wigan. Consultations with their Mathematics Advisers have made significant contributions to the development of the scheme.

The manuscript was prepared through many revisions by Susan Hatfield, Diane Jackson and Jenny Payne, and the staff of Burgess and Longman.

We are grateful to them all.

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Numeracy through problem solving

Plan a Trip is one of a series of modules that have been designed to encourage a new approach to the teaching and learning of numeracy, understood in the original broad sense^(1,2) as

the ability to deploy mathematical and other skills in tackling problems of concern or situations of interest in everyday life.

There is now a general acceptance that people need to learn to *use* the knowledge and skills they acquire at school, and that this requires a shift in the balance of the curriculum to include more real problem solving. This is particularly important for the mathematics curriculum, because the power of mathematics in helping people tackle real problems more effectively, is not often realised.

The Cockcroft Report says

'Most important of all is the need to have sufficient confidence to make effective use of whatever mathematical skill and understanding is possessed, whether this be little or much.' (paragraph 34)

and

'Our concern is that those who set out to make their pupils 'numerate' should pay attention to the wider aspects of numeracy and not be content merely to develop the skills of computation.' (paragraph 39)

TVEI and other recent curricular initiatives have similar aims, emphasising that curricula should contain a strong element concerned with the tackling of practical problems relevant to everyday life and work. The assessment criteria for the GCSE emphasise these aspects too. Employers say that they are primarily interested in people who can use their knowledge sensibly and effectively.

A curriculum component of this kind places new demands on teachers; it needs a broader range of teaching strategies than does the traditional mathematics curriculum, with some new roles for both teachers and students. The scheme has been developed to provide an introduction to such work in the classroom that is both effective and enjoyable for those involved.

What are the skills?

The modules are based on practical contexts which have been chosen to allow students of all abilities to develop general problem solving (or *strategic*) skills in areas of activity such as designing and making, planning and organising, and choosing.

These strategic skills include:

- understanding general ideas and details
- following instructions precisely
- distinguishing between essential constraints and desirable features
- identifying faults
- correcting faults
- generating and listing possibilities (brainstorming)
- developing a rough plan, including: reviewing the prepared suggestions; reaching and recording agreed decisions; maintaining a broad level of description, avoiding excessive detail; identifying needed information and materials; making estimates of quantity and cost; describing, testing and evaluating the plan
- making the final plan, product and/or detailed instructions with comprehensiveness, accuracy, clarity and quality
- implementing the activity with full preparation
- testing and evaluating the plan or product comprehensively.

Various *tactical skills*, more specific to each context, are involved in implementing these strategies; for example, different ways of collecting and recording information are appropriate if you are considering alternative products to buy, or alternative routes to follow.

Technical skills are, of course, required to carry through the solution of problems using the higher level skills described above. Technique is only useful for these purposes in so far as it is *reliable*. This implies much higher standards in this respect than are expected in the traditional curriculum, with a greater emphasis on thorough understanding and checking of whatever techniques are used.

¹ 15–18 A report of the Central Advisory Council for Education (England). HMSO, 1959.

² Mathematics counts. Report of the Committee of Enquiry into the Teaching of Mathematics in Schools under the chairmanship of Dr W H Cockcroft, HMSO, 1982.

Among the mathematical techniques and concepts, of importance in this scheme, are:

- the ability to
 - carry through simple calculations with suitable accuracy, using a calculator where appropriate
 - make estimates
 - make measurements (including number, length and time)
 - draw accurately
 - interpret and display data in a variety of representations (including graphs, maps, timetables and other tables).
- understanding and using some techniques of
 - probability and statistics
 - ratio and proportion
 - geometry in two and three dimensions.
- logical reasoning, including the ability to enumerate alternative possibilities and classify them in various ways.
- research skills, including the collection and evaluation of relevant data.

The relevant mathematical skills are discussed in more detail in each module package. There is also opportunity for the use of other parts of the mathematics curriculum which a student has mastered.

In addition skills from other curriculum areas, such as language and arts, are inevitably called upon, as these are necessary for the presentation of the reasoned arguments which are essential for real problem solving. Since group work is involved, social skills also play their part. Thus, though numeracy is focussed on the deployment of mathematical skills and reasoning in real problem solving, it has a broad cross-curricular aspect.

What is provided?

The scheme is implemented in a modular form, each module being designed to occupy between 10 and 20 hours of teaching time spread over 3 to 6 weeks. Five modules will be available in the first instance. A feature of each module is the importance attached to students working in groups, explaining their ideas and listening to each other, making their own decisions and living with the consequences, reflecting on their experience and learning from it, just as they do in life outside the classroom. While working through the modules, students themselves become responsible for setting and tackling their own problems, rather than simply responding to tasks set by the teacher. Modules are not necessarily staged nor are they dependent upon each other but the sequence which follows is recommended as providing an appropriate progression and a balance of different kinds of context.

The modules in the series are:

- Design a Board Game: in which students design and produce a board game which can be played and evaluated by other members of the class.
- Produce a Quiz Show: in which students devise, schedule, run and evaluate their own classroom quiz.
- Plan a Trip: in which students plan and undertake one or more class trips, and possibly some small group trips.
- Be a Paper Engineer: in which students design, make and evaluate 3-dimensional paper products, such as pop-up cards, envelopes and gift boxes.
- Be a Shrewd Chooser: in which students research and provide expert consumer advice for clients in their class.

Many contexts were considered and tried in the early stages of development, to see which led to the best balance of classroom activities and learned skills. Those that were chosen all have a practical outcome, interesting and relevant to the students' present circumstances. This corresponds with our observation that people best develop the strategic skills of numeracy in the course of solving problems which they see as realistic, stimulating and within their capabilities. The themes selected were found to have general appeal and to require the use of a wide range of skills, whilst not making unreasonable demands on classroom or school organisation.

Discussion with students and observation in the classroom support the expectation that students' problemsolving abilities improve as they work through the series of modules and that skills acquired in one area are subsequently applied in others. Students themselves maintain that they will be able to apply these strategic skills with advantage in tackling further problems as they arise in their lives outside the classroom. Groups of students also suggested many other interesting and worthwhile themes, each of which could form the basis for a further module. These include: planning and running a jumble sale; raising money for charity by sponsored events; planning and running a magazine; setting up a small business; planning a party; designing a bedroom; planning a youth group weekend; making a garden; orienteering; designing and marketing T-shirts.

The scheme provides classroom materials and assessment tasks, together with further support materials to help teachers explore in greater depth the issues and teaching strategies involved. Suggestions for further mathematical development are also included. **Classroom materials,** including detailed teaching suggestions, have been developed to offer a proven approach that has worked well for a representative group of teachers, new to this kind of work, without imposing on them excessive demands of design or implementation. We recognise that, of course, each teacher works in his or her own way in the classroom but most have been found to appreciate detailed, explicit suggestions which they can use, and adapt, in the knowledge that they have worked well for others. Such materials are provided in each module package.

Assessment tasks play an important role in the curriculum, providing targets that help students and teachers recognise objectives more clearly and help them to progress towards them. (The effect of assessment on the curriculum has often been to narrow and distort its aims but, equally, assessment can be used to enhance what is achieved.) In a new curriculum component like this one, assessment is particularly important. Thus assessment tasks are provided throughout these materials. They relate closely to the Scheme of Assessment for the Certificate of Numeracy through Problem Solving offered by the Joint Matriculation Board, but may be used more widely.

The suggestions for further mathematical development provide a variety of ideas, together with discussion on

how and when they might be introduced and linked to the more traditional teaching of mathematical techniques.

Support materials are designed to help teachers with the new aspects of classroom activity and teaching style that this work involves. The materials relate to the three principal differences between this work and the traditional mathematics curriculum - the broader range of skills involved, the practical priorities of numeracy. and the much greater responsibility of the students for their own work. In the traditional curriculum students are largely *imitative*, here they are *autonomous* in deciding on and carrying through their approach to the task. The primary support is provided by the teaching suggestions in the classroom materials and elsewhere in each Teacher's Guide. The support materials, which form a separate package, take this further, sharpening awareness and tackling more fully and deeply the teaching and assessment issues and skills involved. They may be regarded as a do-it-yourself in-service course, designed to be used either on a distancelearning basis by teachers in a school or within LEA or college courses. This material, which is linked particularly to the 'Be a Paper Engineer' module, includes a video of the modules in use, together with comments from teachers and students on the work, its challenges and its benefits.

Introduction to Plan a Trip

Most school trips are organised and run by teachers, and the educational objectives are met by activities which take place at the destination. The students therefore learn little about the processes that go into the original planning. In this module, however, the students take on the responsibility for planning, organising and going on a trip during school time. The destination is largely irrelevant, as the main objective is to increase the students' ability to make, implement and learn from their own decisions and thus feel more confident when moving beyond the immediate surroundings of their own homes, school or town centre. The planning skills developed may also be utilised within other contexts.

The planning process is arranged in four stages.

1. Looking at trips. In a card game simulation, groups undertake and record imaginary trips, encounter problems and errors of judgement, then seek to correct them by better planning. (This involves the strategic skill of 'evaluating a plan and identifying faults in it'.)

2. Making rough plans. Groups share ideas of possible places to go and produce a leaflet explaining these ideas. The class then work together to reach a decision on the best destination and look at possible means of transport. (This involves 'generating lists of alternatives', 'devising a satisfactory rough plan', and 'using and describing a decision making process'.)

3. Making detailed plans. The class lists, and then shares out and undertakes the preparatory tasks that need to be done before the trip can take place. (This involves 'obtaining and interpreting information from a variety of sources', 'identifying omissions in given information', 'placing given jobs in a logical order', 'completing a clear and comprehensive final plan' and 'taking an active part in the planning process'.)

4. Going on your trip and evaluating it. The trip now takes place and, afterwards, the students reflect on what happened. (This involves 'evaluating a plan which has been implemented'.)

Chapter 1 provides classroom materials and teaching suggestions for the sequence of activities.

The range of mathematical techniques required, and the tactical skills needed for their deployment, will depend on the level of ambition in the choice of destination and mode of transport. The range is likely to include

- carrying out simple calculations with money and time
- sequencing preparatory tasks
- selecting and interpreting information presented in various ways (for example, maps, timetables, twoway tables, directories, brochures)
- obtaining information, including the use of letters and the telephone
- drawing up timetables for the trips
- reaching agreement via some kind of voting system.

These aspects are discussed further in Chapter 2, while Chapter 3 is concerned with assessment.



Classroom materials

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Classroom materials

Introduction

This chapter provides a detailed guide to the classroom materials. The suggestions are offered in the recognition that every teacher has an individual style in which he or she prefers to work. Many teachers, however, have found it helpful to be given detailed suggestions which they can then adapt to meet their own needs. This has also enabled us to offer an approach which we have seen working well in a representative range of classrooms.

The classroom materials are centred on the Student's Booklet which is important for the following reasons.

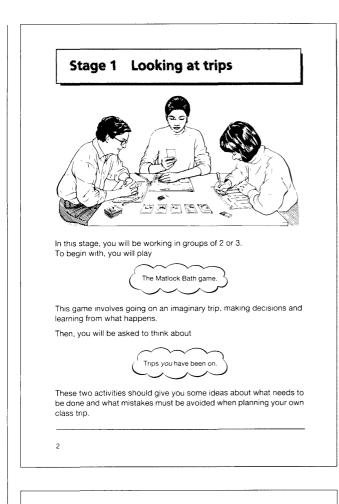
- It provides students with a coherent structure for their work. At any point, it should help students to have an overview of what they have achieved and where they are going.
- Students who are inexperienced in planning often latch on to safe, familiar ideas without carefully considering a range of alternatives. The booklet will help to slow down and stimulate the more impatient or less imaginative students by, for example, asking them to list and discuss a range of destinations and methods of transport before they embark on one particular plan.

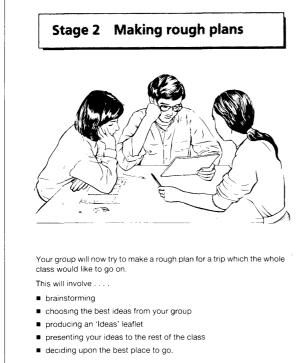
Much of the work involves students working collaboratively. It is often difficult to assess an individual's contribution to the work of a group, so we have also included a number of short assessment tasks, associated with each stage, which provide evidence of what a particular student can do on his or her own. You will find more detailed suggestions on how to use these tasks in Chapter 3. Real problem solving in the classroom demands a different balance of teaching styles and strategies from that in the traditional mathematics curriculum. The emphasis on student-led decision-making will be unfamiliar to some teachers. For this reason, we offer the following suggestions which have been found helpful.

Your role will involve rather less task setting and explaining than you may be used to. Instead, you will be acting more as an adviser and resource, responding to students rather than directing them. It is helpful if you can

- listen to students and ask questions which may help them to clarify their own thinking and move beyond superficial discussions
- encourage students to listen to one another, making sure that the less forceful or less articulate are given the chance to express their views
- help students to pace their work by agreeing target dates by which phases of their work should be completed
- avoid 'taking over' by suggesting your own ideas and making decisions for students. Try to make students feel that it is *their* trip by allowing them to take on as much responsibility as possible.

These suggestions are amplified in the Checklist which may be found on the final page of this book.





Before you start, your teacher will tell you when you can go and how long your trip can take.

q

Summary of activities

Time needed

About 2 hours.

Students' activities

- Playing 'The Matlock Bath Game'. This game simulates a whole trip in an interactive way. Students have to make decisions and experience the consequences. They are also given the opportunity to set their own challenges and become familiar with real timetables and information leaflets. These are group activities.
- Writing about trips they have been on and considering good and bad aspects. This could be an individual activity, possibly for homework, or form the basis for a group discussion.

The teacher's role

- Helping students to understand the game and to record what happens.
- Encouraging groups to discuss the alternatives presented on each card before making decisions.

Time needed

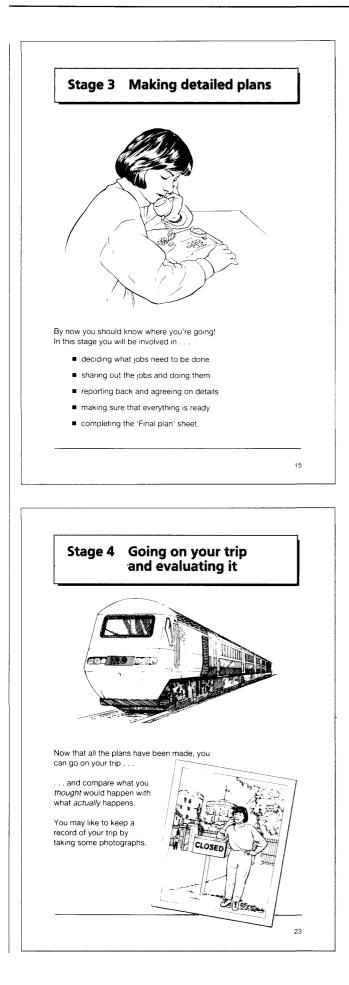
About 2 hours.

Students' activities

- Brainstorming ideas about possible places to go, activities to do and methods of transport. Mainly an individual activity.
- Choosing the best ideas in discussion with the group.
- Producing leaflets which will communicate these ideas to the rest of the class. An individual activity.
- Deciding where to go. A class activity.

The teacher's role

- Making any external constraints clear to students. (For example, the date and duration of the trip.)
- Encouraging groups to be imaginative, but realistic, in their discussions.
- Ensuring that students take each others' views into account, especially when choosing a destination for the trip.



Time needed

This will depend on the complexity of the trip and the size of the class. It may be preferable to spread the work over 2 or 3 weeks (interspersing it with normal class work) as there may be delays in obtaining information.

Students' activities

- Deciding what jobs need to be done. A group activity followed by a class activity.
- Sharing out jobs, doing them, and reporting back on the progress that has been made. Class discussions, interspersed with group activities.
- Making sure that everything is ready, and completing the final plan. A class discussion followed by an individual activity.

The teacher's role

- Helping the students to produce a complete list of jobs.
- Checking that groups are completing their jobs satisfactorily.
- Helping the student who is responsible for coordinating the work of the class.

Time needed

In addition to the trip itself, up to 1 hour will be needed for evaluation.

Students' activities

- Going on the trip.
- Thinking about the trip and comparing what actually happened with the plan. A group activity.
- Evaluating the trip and, in particular, identifying gaps in the planning. An individual activity.

The teacher's role

- Accompanying students on the trip.
- Encouraging students to criticise in a constructive manner.

Preparation

It is perhaps worth emphasising that a 'trip' does not have to mean a day-long coach outing to some far-flung destination. Indeed, an over-ambitious trip may force you to take over too much of the planning, and thus undermine the educational value of the module. A short afternoon visit to a local place of interest using public transport, for example, may provide a more accessible challenge and offer greater opportunities for students to work autonomously. We therefore recommend that, especially for the less confident, you set constraints which encourage students to explore possibilities locally.

Organising a trip out of school raises issues of legal responsibility. Although the students should always feel that it is their trip, legally you (and any accompanying colleagues) will be held responsible. You will therefore have to ensure that school and LEA (where appropriate) policies and procedures are followed correctly. Perhaps if the students were also made aware of these, they might be able to take them into account when suggesting possible plans.

The following checklist suggests some of the things that need to be done before work begins on the module.

- Choose one or two possible 'trip' days. These should fall at least 4 weeks after the beginning of the work.
- Check for possible school calendar conflicts. (This avoids the disappointment of postponing a trip because of, say, a school careers visit.)
- Familiarise yourself with the LEA and school policies on school trips. (These include matters such as advance notice, insurance, staff-student ratios, gender of staff.)
- See and obtain the support of key people (including other staff and the headteacher).
- Check that supply cover is available for the lessons you will miss.
- Find out if there is any money available or if the trip has to be totally self-financing.
- Make a list of the constraints that will be imposed. (For example; 'We must go on Wednesday afternoon . . . , the venture must be self-financing . . . , sorry, I'm just not prepared to go windsurfing!'.)

Equipment needed

When needed	Item	Quantity	Source
Throughout the module	Student's Booklets	1 for each student	supplied
	Envelopes or folders in which to keep work	1 for each student	
	Rough paper	a plentiful supply	
Stage 1	'The Matlock Bath Game'	8 sets for a class of 25	supplied
	Matlock Bath tourist information	1 set for the class	supplied in polythene bag
	Nottingham street map	1 for each student	master supplied
	Local bus and train timetables (optional for this stage)	At least 1 set per class	
	'Record' sheets	3 or 4 for each student (one may be used for the assessment task)	master supplied
	'Trips I remember' sheets	1 for each student	master supplied
Stage 2	'Brainstorming' sheet	1 for each student	master supplied
	'Ideas leaflets'	1 for each student	masters supplied
	Assessment task (if required)	1 for each student	master supplied
Stage 3	'Jobs list' sheets	1 for each student	master supplied
	'Job cards'	1 set for the class	masters supplied
	'Job done' sheets	1 for each job (Approx 20 altogether)	masters supplied
	'Final plan' sheets	1 for each student	masters supplied
	Local travel and tourist information (see below*)	1 set per class	
	Stationery and other resources for organising the jobs (see below†)	1 set per class	

When needed	ltem	Quantity	Source
Stage 3 (contd)	Assessment task booklet (if required)	1 for each student	masters supplied
	Assessment resources:		
	Pre-recorded tape	1 per class	supplied
	Cassette recorder	1 per class	
	National Express coach service leaflet	At least 1 per class	supplied in polythene bag
	Nottingham bus route map	At least 1 per class	supplied in polythene bag
	Local telephone directory	At least 1 per class	
	Local 'Yellow Pages'	At least 1 per class	
	Set of 8 leisure centre job cards	At least 1 copy	master supplied
Stage 4	'Evaluating your own trip' sheets	1 for each student	masters supplied

* In Stage 3, students will be involved in finding travel and tourist information. In order to speed up this process, it is helpful to maintain a file of up-to-date information which may be added to by both you and your students, and which is available for them to use on request. It could, for example, include a selection of bus route maps and timetables, train timetables, local street maps, Ordnance Survey maps of the region, and tourist information leaflets on local places of interest. In addition, students may need access to a telephone.

† The following items of stationery will be needed to help with the organisation of the jobs.

A supply of rough paper

2 small boxes labelled 'Finished jobs' and 'Unfinished jobs' (for storing the 'Job cards' and the 'Job done' sheets)

A supply of paperclips

A large sheet of paper (to make a 'Jobs schedule' poster)

A marker pen

A supply of drawing pins or 'Blu-Tack'

Stage 1 Looking at trips

Introduction

This stage begins with a simulation game based on a variety of alternative trips from Nottingham to Matlock Bath in Derbyshire. This is designed to make students aware of the sorts of problems they may face when they are responsible for planning their own trip. As students play the game, they have to make decisions and experience the consequences of them, while carefully recording their expenditure of time and money. They are also invited either to play the game again, using the cards to make the game work out in a certain way (for example, finding the cheapest possible trip), or to use just timetables and information sheets to plan their own trip to Matlock Bath, starting perhaps from their own school. Finally, students are asked to discuss and write about trips they have experienced at first hand to see what may be learned from them.

Total time needed

About 2 hours.

Organisation and equipment required

The students will need to work in groups of 2 or 3 to play 'The Matlock Bath Game'. At one side of the classroom, the information leaflets from the polythene bag and copies of the 'Matlock Bath' map should be displayed and labelled \mathcal{U} . This represents the 'Tourist information office' referred to in the game.

Each group of students will need one set of cards.

Each individual student will need

- a Student's Booklet
- one 'Record' sheet
- one 'Trips I remember' sheet
- an envelope or folder in which to keep his or her work.

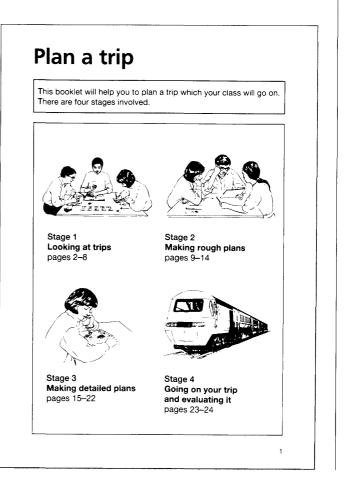
Some students may also ask for

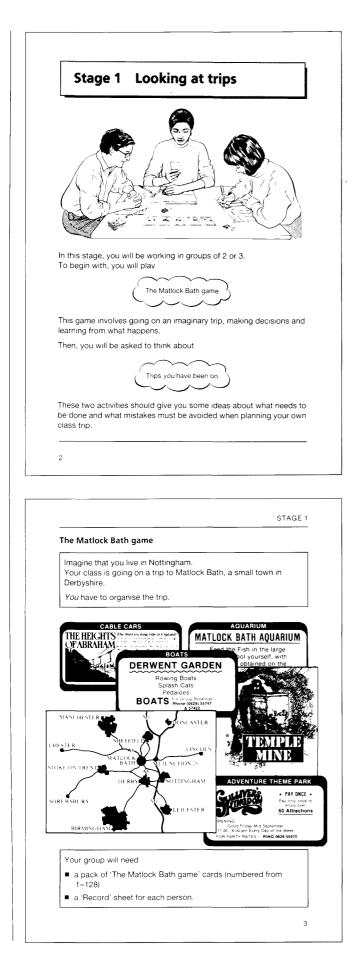
- copies of the Nottingham street map
- local bus and train timetables (for the problem on page 7).

Related assessment criterion

This stage offers students the opportunity to show that they can

(i) evaluate a plan and identify faults in it, (including expenditure of money and time).





Purpose

To introduce the module, to explain the purpose of Stage 1, and to give students some experience of the decisions that must be made and the consequences of making errors in the planning process.

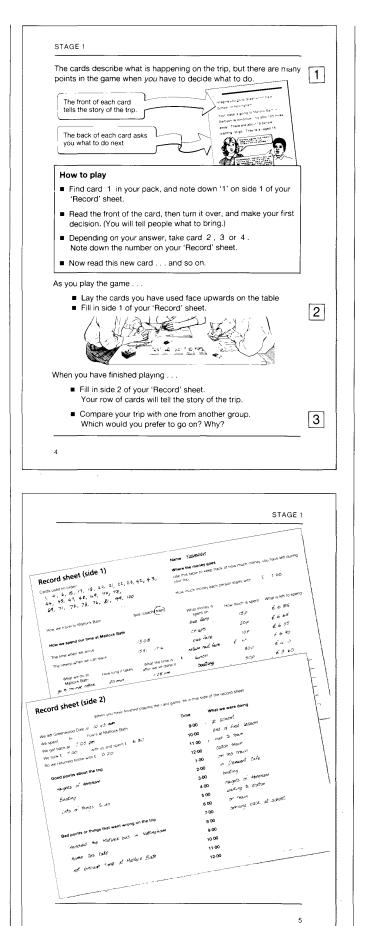
Presentation

A class introduction, followed by group work and concluded with a reflective discussion.

Suggestions and comments

Issue the 'Plan a Trip' Students' Booklets and refer the class to the first page. Briefly explain that during the next few weeks the class will be planning and going on its own trip. Students may find it hard to appreciate that they are actually going to take on this responsibility. (Sometimes this is only fully understood when a problem occurs during the trip itself, and a student turns to you for help. 'Which way do we go now, Miss?' 'I don't know, you have to make the decisions!'.) Begin therefore by emphasising that it will be *their* trip, not yours. The constraints on the trip (for example, the date and duration) should be made clear right from the start so that students are encouraged to be realistic in their ambitions. They may, therefore, need to consider trips that are more localised and less expensive than those which may have been organised for them in the past.

Issue each group of students with a pack of Matlock Bath cards and some 'Record' sheets. Make sure that everyone understands the purpose of the game. The 'Record' sheets are included so that each group can keep track of the money and time spent on the imaginary trip.



- 1 Read through the instructions for playing the game. Check that everyone understands how to use the 'Record' sheet. You could start all the students off together by asking them to write '1' on the 'Record' sheet, then read card 1 and discuss the options given on the back. Students should then be able to continue the game in their groups, following the instructions on the cards.
- 2 Some students become so involved in playing the game, that they forget to keep their 'Record' sheets up to date or their used cards displayed separately from the rest of the pack. Remind them of these points so that they will be able to review the 'trip' when it has ended, using side 2 of the 'Record' sheet.

On the following pages, we have provided a network which displays every possible route through the cards. This can be used to check that card sequences are correct so that help may be given if a group gets into difficulty.

3 When two groups have completed their trips they should be brought together for discussion. In particular, they should compare their 'Record' sheets and try to identify any particularly good or bad decisions that were made.

The Matlock Bath Game

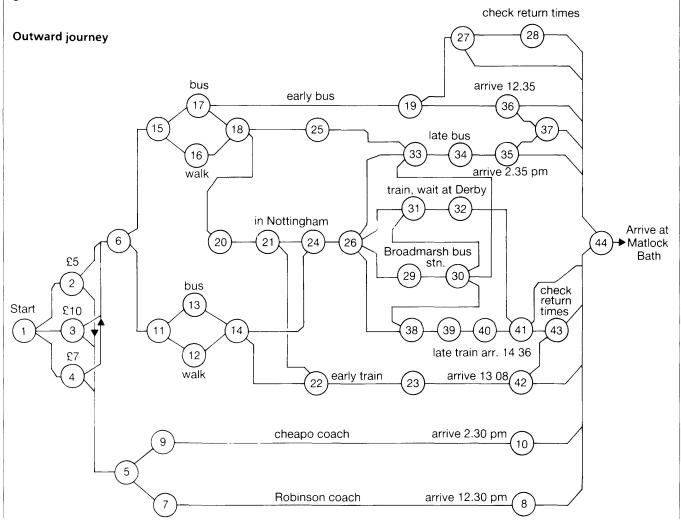
The three networks below illustrate all the routes through 'The Matlock Bath Game'. In general, routes lead from lower to higher numbers, with routes arriving at circles on the left and leaving on the right. All the data used were correct for the summer of 1987.

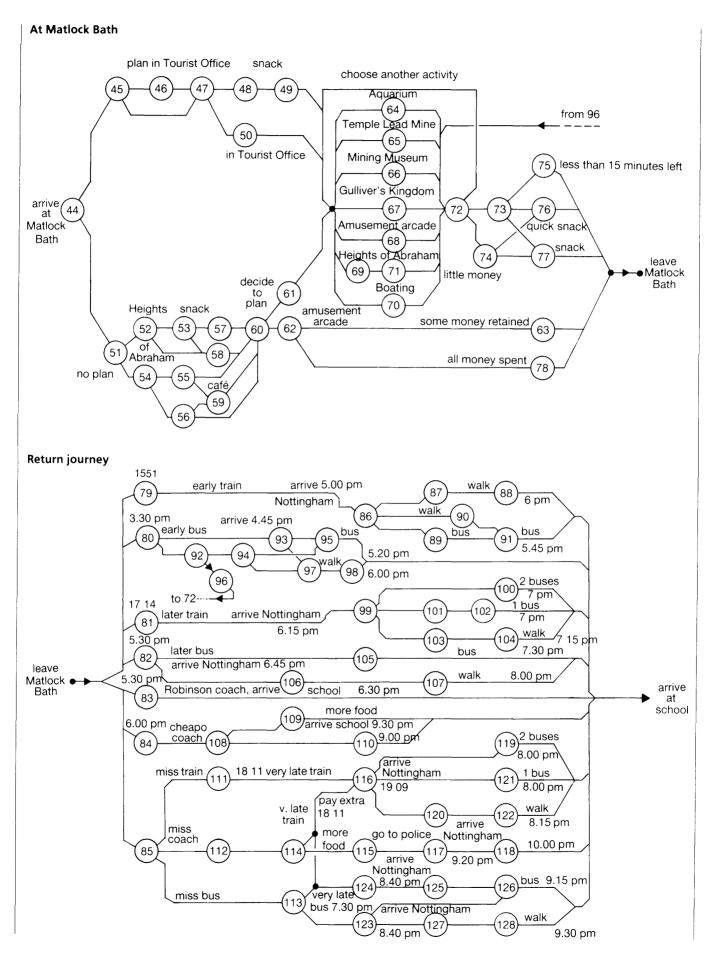
Although every effort has been made to ensure that all the complete routes are internally consistent, there are inevitably some which are less so than others. Your students will be keen to point these out to you. You or your students may wish to revise, improve or extend the game using the data in the pack.

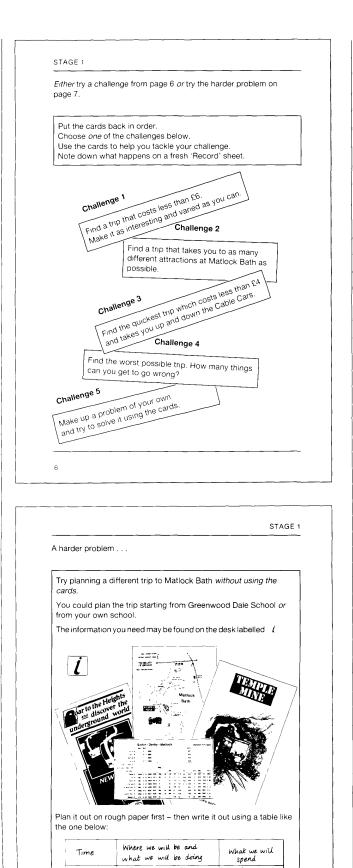
You may like to try creating a similar game using tourist information relevant to your own locality, in which case the following suggestions may be of help.

- Select a single destination which has a variety of alternative activities.
- Ensure that you can travel to and from this destination using a variety of alternative routes, and that the fares are comparable.

But be warned, the time involved in constructing such a game is considerable!





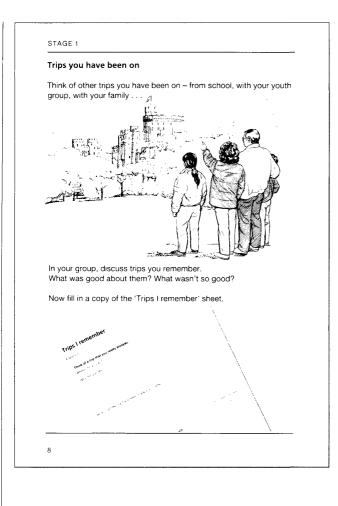


7

The challenges on page 6 encourage the students to think more carefully about the planning decisions that they make in the game. If two groups take on the same challenge they could compare their results. Encourage students to set and try to solve their own problems using the cards.

The problem on page 7 is more difficult as it involves using timetables and information leaflets without the support of the cards. Groups that do this should keep in mind the trips they simulated with the cards so as to remember the necessary steps in planning.

Planning a trip from the students' own school to Matlock Bath is an interesting exercise, wherever the school is situated. It makes the task more real to them. If the school is far away, it is interesting to find the best route by train and whether or not it is possible to get there and back in a single day. From some places it may be necessary to book overnight accommodation!



The final activity in this stage offers students the opportunity to think reflectively about other trips they have been on. The activity could begin with a short class discussion. Students should be encouraged to notice which problems were caused because of bad planning and which were unfortunate occurrences that could not have been anticipated (for example, a puncture). It may also be worth asking students to recall how such problems were overcome.

Each student should fill in a 'Trips I remember' sheet, recalling his or her experiences.

Assessment task for Stage 1

The 'Record' sheet

The assessment task which relates to the Stage 1 assessment criterion is described below. This task may be helpful when deciding whether or not a student can

(i) evaluate a plan and identify faults in it (including expenditure of money and time).

Chapter 3 contains a more detailed discussion of assessment issues, including suggestions for marking and record keeping.

This task requires each student to work on one of three alternative routes through the Matlock Bath cards, completing a 'Record' sheet during the process. Select from the Matlock Bath packs, sufficient sets of the following cards, so that each student undertaking the assessment has a set.

The three sets are

Set A 2, 6, 15, 17, 19, 27, 44, 51, 54, 56, 60, 62, 63, 80, 93, 95.

- Set B 3, 5, 9, 10, 44, 51, 52, 53, 58, 60, 62, 78, 84, 108, 110.
- **Set C** 4, 6, 11, 13, 14, 24, 26, 31, 32, 41, 44, 45, 46, 47, 50, 69, 71, 72, 73, 75, 79, 86, 89, 91.

Issue each student with a 'Record' sheet and arrange the students so that neighbouring students have different card sets.

Each student should fill in a 'Record' sheet while working through one of the three sets.

Card number 44 is common to all 3 sets, and as there will be insufficient copies, you could either summarise the contents of this card on the blackboard or photocopy enough copies for everyone. Cards 6, 51, 60 and 62 occur in 2 of the 3 sets, so you may need a few extra copies of these, too.

You will need to issue the following additional information to clarify the decisions to be made on some cards, as follows

Set C 26 - have snack costing 60p

- 32 have snack costing 60p
- 47 it takes 20 minutes to go to the Tourist Information Office
- 71 you spend 60p at the Woodlanders and you reach the bottom of the cableway at 3.40 pm.

The three sets are broadly comparable, though set C is probably the hardest to work through.

Solutions to the assessment tasks for Stage 1

Illustrated below is a typical solution to each of the three tasks. The correct completion of side 1 is likely to show little variation from the examples given here, but the comments on side 2 will depend to an extent on the student's own view of what constitutes a good or bad point.

Some students may add extra time allowances for walking from one activity to the next at Matlock Bath and so produce slightly different time schedules from those shown here.

Set A

Record sheet	: (side 1)		Name		
Cards used (in order) 2 , 6, 15, 17, <u>1</u> 60, 62, 63, 8	<u>9,27,44,51,</u> 30,93,95	54, 56,	Where the money go Use this table to keep your trip.	es htrack of how much mo	ney you have left durin
How we travel to Matlo	 ck Bath	busy coach/train	How much money eac	ch person starts with	£ 5 00
			What money is spent on	How much is spent	What is left to spend
low we spend our tin	ne at Matlock Bath		Bus fare	15p	£ 4 · 85
he time when we arriv	e	12.35	Bus fare	1 75	£3 10
'he time(s) when we ca	n leave	3.30, 5.30 _{pm}	Heights of Abra	ham 1 95	£1.15
What we do at Matlock Bath	How long it takes	What the time is after we've done it	anusement arcade	£ 1.00	م15 م
cable car (Height's	2 hour	105 pm	Bus fare	15p	
checking	4 hour	1.20 pm			
Imusement	2 hours	3.20 pm			
walk to catch bus	10 min	3 30 pm			
1		• • • • • • • • • • • • • • • • • • • •	L	£ 5.00	t

When you have <i>finished</i> playing the card	game, fill in this	side of the record sheet.
left Greenwood Dale at 10.45 am	Time	What we were doing
spent 3 hours at Matlock Bath.		
got back at 5. <u>20 pm</u> . took £ . 5 with us and spent £ <u>5</u>	9.00	+
we returned home with \mathfrak{L}	10.00	+
		- bus to town
ood points about the trip	12.00	- on bus to Matlock Bath
The cable car	1.00	- on cable car
ne carre car	2.00	- amusement arcade
	3.00	- amusement arcade
	4.00	- on bus back to Nottingho
		at lus stop on Long Row E
		+ home
ad points or things that went wrong on the trip	7.00	, unice
id not take enough money	8.00	
asted our Heights of abraham ticket		
spent too much on the bus fare	9.00	†
lident plan what to do	10.00	+
	11.00	
	12.00	+

M2

Set B

Record sheet (side 1)		Name			
Cards used (in order) 3,5,9,10,4 78,84,108,		<u>, 58, 60, 62,</u>	Where the money goe Use this table to keep your trip.		ney you have left durin
How we travel to Matloc	ck Bath	bus (coach) train	How much money each	person starts with	£ /0
			What money is spent on	How much is spent	What is left to spend
How we spend our tim	e at Matlock Bath		Coach	£2.50	£ 7.50
The time when we arrive	3.	2 30pm	Heights of abra	ham£1.95	£5.55
The time(s) when we car	n leave	5.30 pm	-	75p	
			amusement arco		
What we do at Matlock Bath	How long it takes	What the time is after we've done it			
Cable car (Heights	am) the	3.00 pm			· · · · · · · · · · · · · · · · · · ·
snack	20 mins	3.20 pm			·
mine and cavern	e I hour	4.20 pm			
amusement arc	ade 55 mins	5.15 pm			
walking	10 min	5.25 pm			
wait for coach	35 min	6 00 pm			
			Total amount spent	£ 10 00	

When you have finished playing the car	d game, fill in this	side of the record sheet.
/e left Greenwood Dale at 12.00	T '	
/e spent3 ź hours at Matlock Bath.	Time	What we were doing
le got back at $\frac{9.00 pm}{}$	9.00	+
/e took \mathfrak{L} / \mathcal{O} with us and spent \mathfrak{L} / \mathcal{O}	10-00	+ at school
o we returned home with \mathfrak{L} O	11.00	- at school
Good points about the trip	12.00	- getting on the coach
The cable car		- on the coach
The mines and cavern	2.00	- on the couch
	3-00	- getting off cable cars
		- going around the mines
		- amusement arcade
	6.00	get on coach
Bad points or things that went wrong on the trip		- coach broken down
bad coaches kept breaking down	8.00	+ other coach arrives
we didn't plan properly		- anive home
we spent too much on amusements	10.00	1
very hungry when we got home		
Too much time spent travelling	11.00	
	12.00	+

M2

Set C STAGE 1

	47, 50, 69,	31, 32, 41, 71, 72, 73, 75,	Where the money goe Use this table to keep your trip. How much money each	track of how much mor	ney you have left during $\hat{\Sigma} = 7 \cdot 00$
How we travel to Matloo	ck Bath	bus/coach train			
			What money is spent on	How much is spent	What is left to spend
How we spend our tim	e at Matlock Bath		bus fare	15p	6 85
The time when we arrive	ə	2:40pm	crisps and cake	50p	6 35
The time(s) when we ca	n leave	1551 1714	snack	60p	5·75
			train fare	£1 65	4.10
What we do at Matlock Bath	How long it takes	What the time is after we've done it	snack	60p	3 50
go to tourist info	20 min	3.00 pm	Heights of abrat	ram£1.75	1 75
choosing what to		3.15 pm	cafe	60p	1 15
Heights of abrah		3.40 pm	bus fare	10p	1 05
run for train	10 min	3.50 pm	bus fare	م15	0.90
catch train	1 min	3.51 pm			
			Total amount spent	£ 6 10	

When you have finished playing the carc	game, fill in this	s side of the record sheet.
e left Greenwood Dale at 10.45 am		······································
e spent I hr II min hours at Matlock Bath.	Time	What we were doing
e got back at <u>5 45 pm</u>	9.00	+
e took \pounds 7.00 with us and spent \pounds 6.10	10.00	- at school
b we returned home with $\pounds _ O \cdot 9O$	11.00	- on the bus
Good points about the trip	12.00	- having snack
trip on a cable car		- arrive at Derby station
ing sit a table at	2.00	- on Derby station
	3.00	+ go to tourist information office
	4.00	- on train back
	5.00	- reach Nottingham station
		- arrive home
Bad points or things that went wrong on the trip	7.00	
missed train	8.00	+
ong wait at Derly station	9.00	+
caught the train back too early	10.00	+
shouldn't have had so many snacks	11.00	-
	12.00	

M2

Stage 2 Making rough plans

Introduction

The activities contained in this stage develop a number of important strategic skills which may be applied to other planning and organising tasks. These activities, which many students are likely to find unfamiliar, include

- exploring a wide range of alternatives before deciding on a particular idea
- considering the needs and interests of all those involved, rather than making a personal choice
- making reasonable guesses about unknown facts in order to inform a decision
- presenting an idea to other members of the class
- discussing various decision-making processes and using them to choose the 'best' trip destination.

Total time needed

About 2 hours, but possibly longer if reaching a class decision proves difficult.

Organisation and equipment required

Students will need to work in groups of 2, 3 or 4 for most of this stage. As the work progresses, groups could be re-formed according to their preferred trip destination.

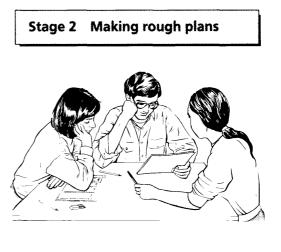
Each student will need

- a 'Brainstorming' sheet
- an 'Ideas leaflet'.

Related assessment criteria

This stage offers students the opportunity to show that they can

- (ii) generate lists of alternatives,
- (iii) devise a satisfactory rough plan (including sensible costings and time schedules),
- (iv) use and describe a decision-making process.

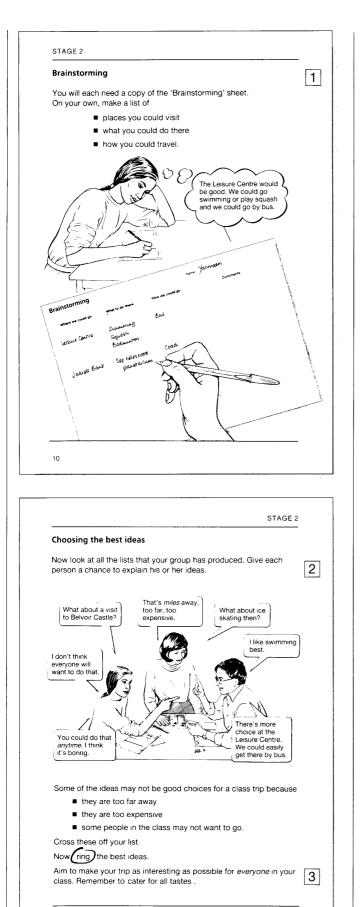


Your group will now try to make a rough plan for a trip which the whole class would like to go on.

This will involve . . .

- brainstorming
- choosing the best ideas from your group
 producing an 'ideas' leaflet
- producing an ideas learner
 presenting your ideas to the rest of the class
- presenting your ideas to the rest of the of
 deciding upon the best place to go.

Before you start, your teacher will tell you when you can go and how long your trip can take.



11

Purpose

To give students the opportunity to think of a wide range of possibilities before sharing their ideas in a group.

For everyone to share ideas and reach agreement on which ideas are worthy of further development.

For students to learn how to listen to and discuss constructively with one another.

Presentation

Class discussion, followed by individual reflection and then by group discussion.

Suggestions and comments

1 You may like to introduce the 'Brainstorming' activity by asking for one or two ideas for each of the different sections on the sheet, and listing these on the blackboard.

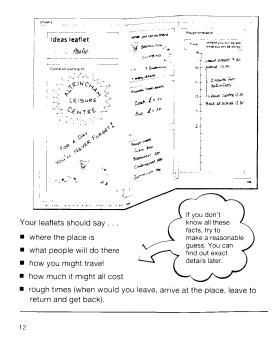
Encourage students to fill in as many ideas as they can, before discussing them. This will ensure that every student has something to contribute to the group discussion which follows.

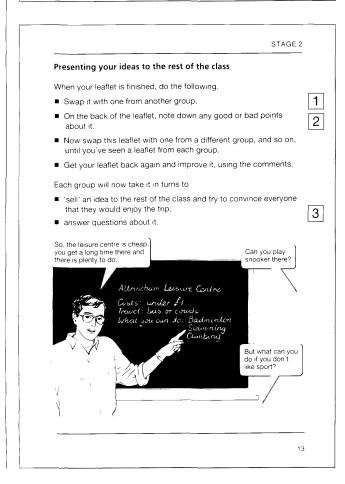
- 2 This may need emphasising, as there is sometimes a tendency for one or two people in a group to dominate the discussion, by pushing their own ideas forward and ignoring those suggested by other students.
- 3 Students often find it hard to devise a suitable trip which both satisfies the external constraints and caters for the interests of other members of the class. Emphasise that if they fail to do this, then there is little likelihood of their ideas being adopted.

STAGE 2

Producing an 'Ideas' leaflet

In your group, look at the ideas that are ringed. Try to decide which is the best choice for a class trip. Each person in your group must then fill in an 'Ideas' leaflet explaining this choice. (You may disagree on some details, but this doesn't matter.)





Purpose

To offer students the opportunity to make a rough plan for a trip, check its feasibility and persuade the rest of the class that it is a good idea.

Presentation

Group discussion followed by individual work and a group presentation to the whole class.

Suggestions and comments

At this point, it may be necessary to rearrange the groups slightly so that each group is now working on a single trip choice.

Each student should fill in a copy of the 'Ideas leaflet'. This should contain sufficient information for the class to make a decision as to the feasibility of the trip and should be presented in an attractive and persuasive manner.

Some students may have difficulty in estimating costs and times. Encourage them to compare the information they need with practical knowledge that they already possess. For example,

'it takes the bus half an hour to get into town. The leisure centre is about twice as far so it will probably take about an hour to get there . . .'

Students should not spend too much time researching information for this activity, as most of these suggestions will not be used for the final class trip. However, promising ideas that are not chosen could form the basis for a small group trip which could take place out of school time.

- 1 You will need to organise the exchanging of leaflets so that everyone has a chance to see a leaflet from each of the other groups.
- 2 Some students instantly dismiss ideas that are not their own. They should be encouraged to comment on *every* idea in a detached, objective manner and perhaps think of ways in which their own preferences could be incorporated into someone else's trip.

3 Each group should be given a few minutes to present its ideas to the rest of the class, leaving time for questions at the end.

<text><text><text><list-item><list-item><text><text><image>

Purpose

To consider alternative decision-making methods and then to decide corporately on the best place to go for the trip.

Presentation

Class discussion.

Suggestions and comments

Begin by reminding the class of the external constraints that the trip has to meet, and then ask students to suggest alternative decision-making processes. List these on the board. For example,

'We could toss for it'

'Show of hands'

'Secret ballot'

'Put these ideas in order of preference'

'Eliminate the least popular ideas'.

It is worth taking time to use two or three of these methods to see if the same result emerges.

If the majority of the class favour the same destination, the decision may be straightforward. The class should still, however, consider carefully any minority views and try to take them into account.

If there is no clear decision, students may need to consider making compromises or revising their proposals.

As a last resort it may be possible, in some cases, to have two trips, or alternative destinations within one trip.

Assessment tasks for Stage 2

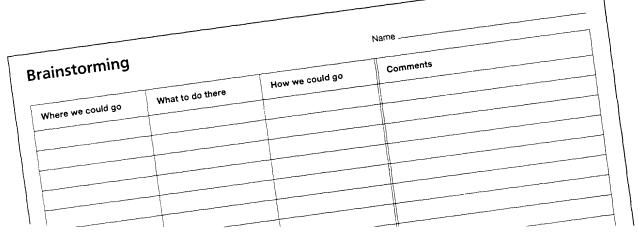
There are 3 tasks that relate to the assessment criteria for Stage 2. The tasks may be helpful in deciding whether or not a student can

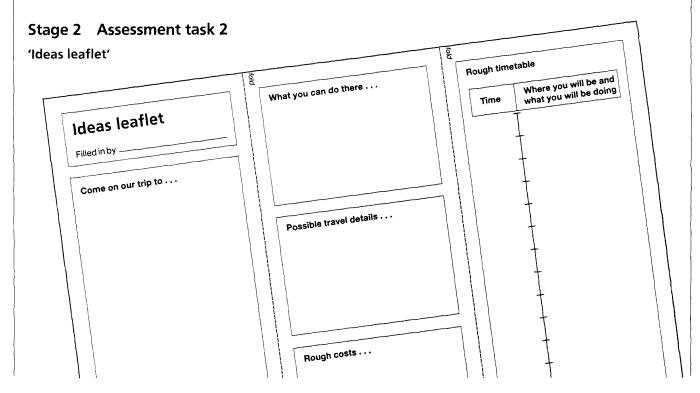
- (ii) generate lists of alternatives,
- (iii) devise a satisfactory rough plan (including sensible costings and time schedules),
- (iv) use and describe a decision making process.

Tasks 1 and 2 should already have been completed during the normal course of the work. They help in assessing criteria (ii) and (iii) respectively. Task 3 is new and may be completed at the end of Stage 2. This task is designed to assess criterion (iv).

Stage 2 Assessment task 1







a) The ice rinkb) Zooc) Bowling alley	ix different places have been sug d) A castle e) Snooker hall f) Swimming pool	
In order to choose between thes		
Each person is given a list, and t This is what they write:	hey write down their preferences	5.
Sanjay	John	Claire
 a) Ice Rink 6th choice b) Zoo 1st choice c) Bowling 3rd choice d) Castle 2nd choice e) Snooker 4th choice f) Swimming 5th choice 	 a) Ice Rink 1st Choice b) Zoo 2nd Choice c) Bowling 5th Choice d) Castle 4th Choice e) Snooker 3th Choice f) Swimming 6th Choice 	 a) Ice Rink 6th choice b) ZOO 5th choice c) Bowling 1st choice d) Castle 2nd choice e) Snooker 4th choice f) Swimming 3nd choice
Mike	Elaine	Jenny
a) Ice Rink 4th choice b) Zoo 6th choice c) Bowling 5th choice d) Castle 3th choice e) Snooker 1st choice f) Swimming 2th choice	 a) Ice Rink Gm choice b) Zoo 3rd choice c) Bowling 2rd choice d) Castle [st choice e) Snooker 4m choice f) Swimming 5m choice 	 a) Ice Rink 6th choice b) Zoo 5th choice c) Bowling 4th choice d) Castle 2th choice e) Snooker 3th choice f) Swimming 1st choice
Which place would be the best ch Explain how you get your answe		

A discussion of this task appears on page T 79.

33

Stage 3 Making detailed plans

Introduction

This stage involves the detailed planning of the trip. When the class has agreed on the list of jobs that need to be done, they are shared out and worked on by small groups of students. Many of these tasks involve the use of mathematical skills (reading timetables, estimating costs and so on). Students should be encouraged to use whatever skills they possess, but they may need to learn others to increase the efficiency and reliability of their planning. At various stages, groups will need to report back on their progress and ask advice from the rest of the class. At the end of the stage a complete detailed 'Final plan' is drawn up.

During this stage, there may be times when students are not fully occupied. For example, they may be unable to start a job until an earlier one has been completed. There are several ways this 'dead time' can be used constructively.

- The first six assessment tasks can be organised as a 'circus' of practical activities which may be attempted at any time and in any order by individual students. They are described more fully below.
- Students may like to plan small-scale 'group trips'. (These trips could be based on the ideas from Stage 2 which were not adopted and could take place out of school time.)
- The work on this stage can be spread over 2 or 3 weeks, interspersing it with work of a different kind altogether.

Total time needed

About 2 to 3 hours, possibly spread out over 2 or 3 weeks.

Organisation and equipment required

Initially the whole class will need to work together in teacher-led discussion. The rest of the work is done in small groups.

You will need

- 1 'Jobs list' sheet for each student
- 1 set of 'Job cards' (folded to A5)
- A supply of about 20 'Job done' sheets
- 1 'Final plan' sheet for each student.

You should also provide

A file of local travel information (containing street maps, bus and train route maps, timetables and so on)

Access to a telephone and local telephone directories

A supply of rough paper

2 small boxes labelled 'Finished jobs' and 'Unfinished jobs' (these are for storing the 'Job cards' and the 'Job done' sheets)

A supply of paperclips

A large sheet of paper (to make a 'Jobs schedule' poster)

A marker pen

A supply of drawing pins or 'Blu-tack'.

In addition, the assessment tasks require

- 1 pre-recorded tape of a British Rail talking timetable
- 1 cassette player
- 1 National Express coach service leaflet
- 1 Nottingham bus route map
- At least 1 local telephone directory
- At least 1 'Yellow Pages' directory
- At least 1 set of the 8 small 'Leisure centre job cards'.

The instructions for setting up the assessment 'circus' is given on page T40.

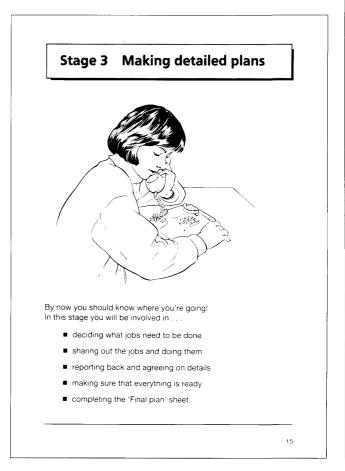
Related assessment criteria

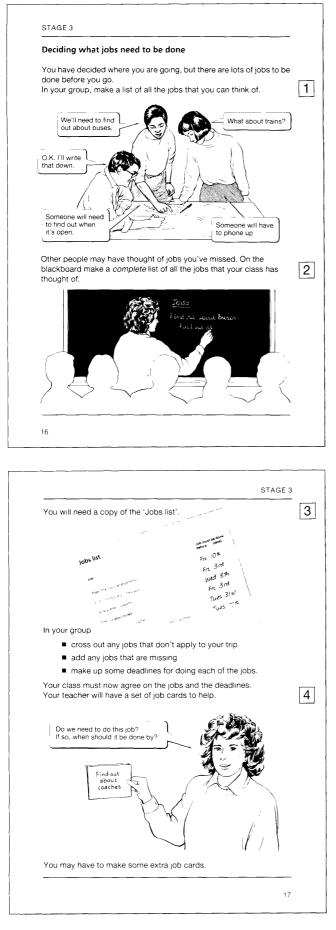
This stage offers students the opportunity to show that they can obtain and interpret information from

- (v) a telephone directory,
- (vi) aural and written timetables,
- (vii) a street map,
- (viii) a route map,

and can

- (ix) identify omissions in given information,
- (x) place jobs in a logical order,
- (xi) complete a clear and comprehensive final plan,
- (xii) take an active part in the planning process.





Purpose

To enable students to decide what jobs need to be done, when they need to be done by, and to organise a procedure for sharing them out and doing them.

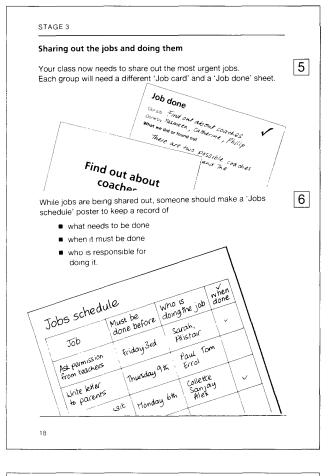
Presentation

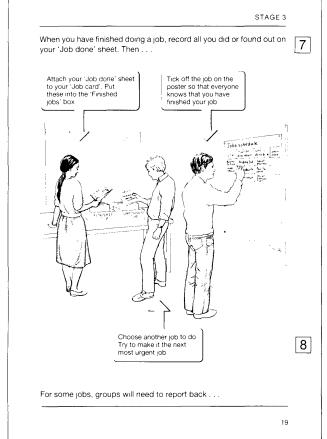
Group work followed by class discussion.

Suggestions and comments

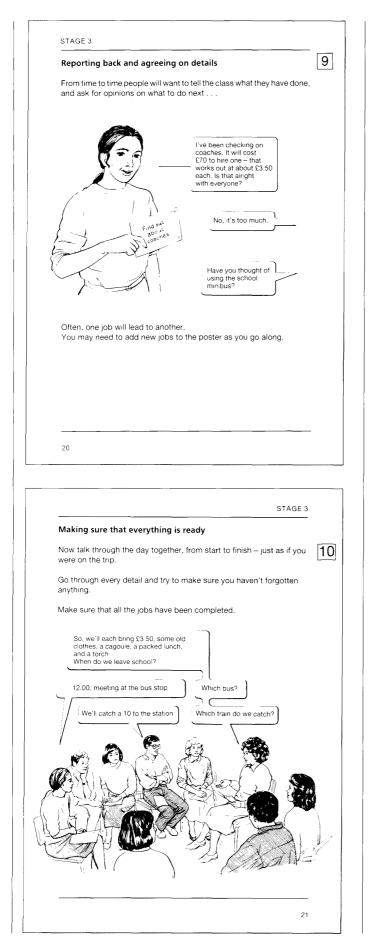
- 1 Issue each group with some rough paper and ask students to note down all the jobs that they can think of which they need to be done before the trip can take place. For further ideas, they could also think back to 'The Matlock Bath Game' and recall what happened and what was done and decided.
- 2 When groups have completed their lists you, or a member of the class, could write the ideas on the board. Working through the trip step by step may help to organise these ideas.
- 3 The 'Jobs list' is provided to save students from having to copy down laboriously the jobs – it also serves as a check that vital jobs have not been forgotten. The groups should start to think about deadlines and thus begin to consider the order in which these jobs should be done. Encourage students to fill in these dates by working backwards from the date of the trip itself.
- 4 There is a 'Job card' corresponding to each of the jobs listed. It is helpful to use these to agree on the actual jobs that need to be done. They could then be sorted, initially, into two piles; those that can be done immediately and those that must wait until other jobs have been completed. New 'Job cards' may need to be written at this point.

The role of job coordinator is crucial. It is best if a student or pair of students takes on this task, but you may prefer to do it yourself. In this case it is worth removing the coordinator job card from the pack, beforehand.





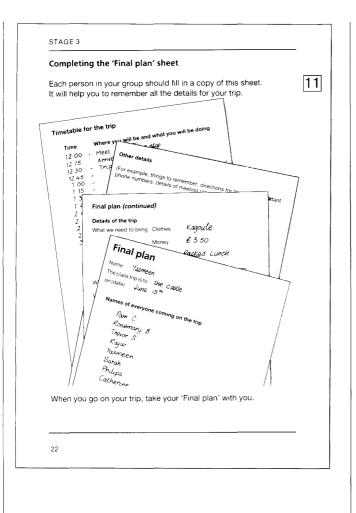
- 5 The most urgent 'Job cards' should now be shared out among the groups. These are likely to include those to do with asking permission and finding out travel details. The remaining cards should be stored in a box (labelled 'Unfinished jobs') at one side of the room.
- 6 The 'Jobs schedule' poster is a suitable task to give to the job coordinator. You may need to help in checking deadlines and ensuring that everyone has something to do.
- 7 Students should write complete summaries of what they have done on the 'Job done' sheets, and attach them, together with any other relevant details (maps, timetables etc), to their 'Job cards'. (If the 'Job cards' are folded in half, to A5 size, then these can be tucked inside and fastened with a paper clip.) These should then be placed in a second box (labelled 'Finished jobs') at the side of the room, for future reference by other class members.
- 8 The coordinator may like to take on the responsibility for allocating jobs. If no new jobs are available, then the students could take this opportunity to attempt some of the assessment circus, or work on their own group trips.



9 Groups should report back whenever a class decision needs to be made, but you may also ask groups to report back more regularly, for example, at the beginning of each lesson. This will keep the momentum going and keep everyone in touch with the complete plan. Be prepared to offer back-up help to ensure that the information is presented clearly to everyone. It will help if you put key questions to the group to help it clarify its presentation. Make sure that someone records any decisions that are made.

If new jobs emerge from the ensuing discussion, you (or the job coordinator) may need to prepare some new 'Job cards'. You may need to add hints on the back.

10 When every job has been completed the class should check that nothing has been forgotten by talking through the whole trip from start to finish.



11 While the plan is fresh in everyone's mind, each student should carefully complete a 'Final plan' sheet. This will help to ensure that everyone feels involved and knows exactly what will happen on the day of the trip. Encourage students to question each other if they are still unclear about any details. Each person should feel confident that she or he could run the trip by themselves.

Assessment tasks for Stage 3

There are seven tasks associated with this stage. Assessment tasks 1 to 6 may be attempted in any order and at any time during Stage 3. Assessment task 7 should already have been completed in the normal course of the work. These tasks may be used to assess whether or not a student can obtain and interpret

- (v) a telephone directory,
- (vi) aural and written timetables,
- (vii) a street map,
- (viii) a route map,

and can

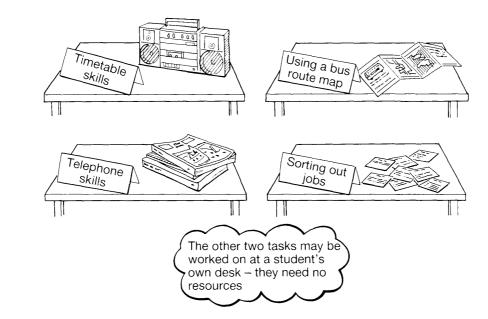
- (ix) identify omissions in given information,
- (x) place jobs in a logical order,
- (xi) complete a clear and comprehensive final plan,

(xii) take an active part in the planning process.

Some suggestions on organising tasks 1 to 6

(It will be convenient to duplicate these tasks back to back to form eight-page A4 booklets.)

As four tasks require resources which will not be in plentiful supply (for example telephone directories), we suggest that, while students are working on Stage 3, you set these tasks up on four desks at the back of the room. (If you have duplicates of resources, then you could of course set up more desks for each.) Each desk should be clearly labelled:



Whenever students are stuck for something to do, they can collect their assessment booklets from you, and you can then direct them to work individually on these tasks at the appropriate desks. When a student has finished a task, this can be recorded on the cover sheet and he or she may then either attempt a second task or return to Stage 3. In the latter case, the assessment booklet could be returned to you for safekeeping.

STAGE 3 Stage 3 Assessment tasks Name. Class _ This booklet contains six tasks. You can do them in any order and at any time during Stage 3. They do not need to be done at one sitting, but may be spread over several lessons. If you have finished a task and do not want to do another one straight away, please return this answer booklet to your teacher. When you finish a task, put a tick against it below: 1. Telephone skills 2. Timetable skills 3. Using street plans 4. Using a bus route map 5. Asking for permission 6. Sorting out jobs Notes for the teacher Masters M25 to M32 should be duplicated back-to-back to form an 8 page booklet. The following resources will be required: Task 1. A copy of a local telephone directory* and a 'Yellow Pages'*. Task 2. A pre-recorded tape of a 'British Rail' talking timetable, a cassette player* and a National Express coach service leaflet. Task 4. A copy of the Nottingham City bus service route map. Task 6. A set of 8 leisure centre job cards (see M33). The items marked * are not included in the module package. Please refer to page 40 in the Teacher's Guide for guidance on setting up these tasks.

Page 1

M25

-

STAGE 3 ASSESSMENT TASK 1

You will need a copy of your local telephone directory	and a copy	of your local 'Yellow Pages'.
 Suppose that you and 6 friends are planning a trip to th to find out travel information. Look up the following boxes. 		
		Train
a) Local passenger train enquiries.	Number:	
		Bus
b) Local bus station, for times of buses which pass	Number:	
<i>close</i> to your school.		Тахі
c) A local taxi service. Write down the <i>name</i> of the taxi company as well.	Name:	
	Number:	
		Mini-bus
d) A local mini-bus hire firm. (You only need a bus	Name:	
for 7 people.) Write down the name of the firm as well.	Number:	
 Suppose that you also want to telephone the zoo. Y number is not in your phone book because it's too fa 'Directory Enquiries' to find the number. 		
Milet surplus is (Disseters Essurision)	Number:	
What number is 'Directory Enquiries'	Number.	
 Suppose that you want to ring a friend who is on holida that the phone number is Falmouth 53839. 	y at a hotel i	n Cornwall. They have told y
		Hotel
What number should you dial? (Give all 9 digits)	Number:	

STAGE 3 ASSESSMENT TASK 2

You will need a tape recording coach service leaflet.	of the British Rail talking time	table and a National Express
nagine that you are planning a ottingham as soon as possible a 00 p.m. You can go either by tra	fter 9.00 am and you want to be	
II in this table to compare the tw	o methods of transport.	
	Listen to the tape to find out train times. (Turn the tape over for return times.)	Use the leaflet to find out coach times.
	Train	Coach
Nottingham to London (outward journey)		
What time would you leave Nottingham?		
What time would you arrive in London?		
London to Nottingham (return journey)		
What time would you leave London?		
What time would you arrive at Nottingham?		
How long would you have in London?		
/hich method of transport would y /hy?		
•	need before making a decision	?

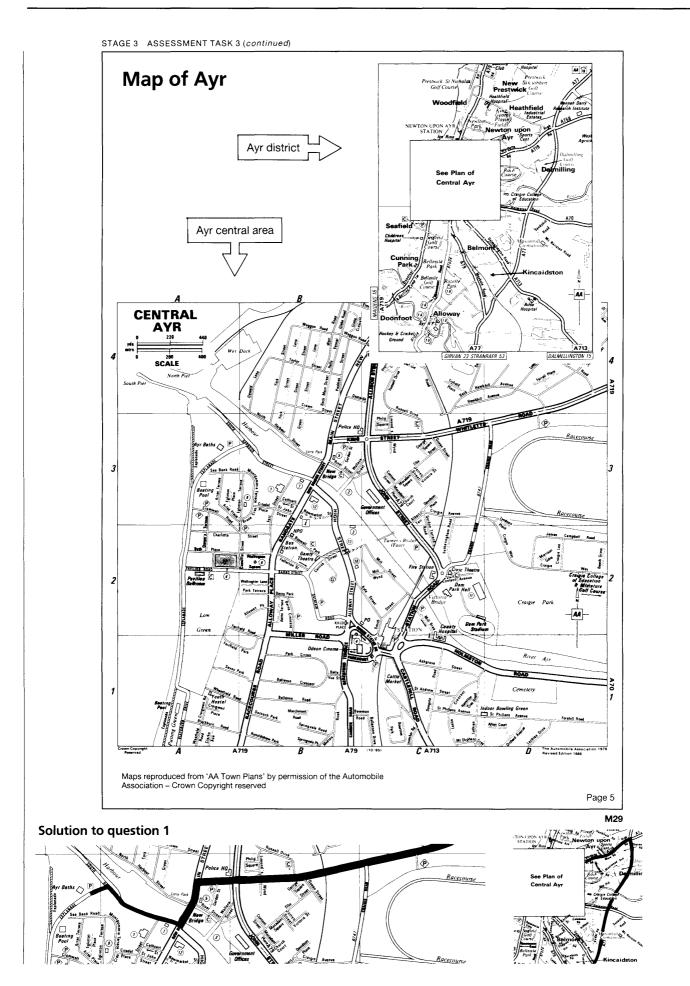
M27

	You will need the Ayr maps.
	Your family is on holiday near Stranraer in Scotland, and is planning to go to the swimming bat n Ayr.
	You are given these directions.
	Go along the A77 road from Stranraer until you pass the golf course at Dalmilling. Then turn left at the next junction and carry on to the end of the road. Turn left, cross the bridge and then turn right. Take the second turning on your left and you'll see the swimming baths on your right.
ę	Show this route clearly on the two maps.
	n the space below describe in words a shorter way of getting to the swimming baths from t A77 from Stranraer.
ł	Keep your instructions as simple as possible.

M28

Solutions to question 2

Any route that is more direct than that given above is acceptable, for example "Turn left along the A79. Continue through the town to the end of the High Street, turn right then left and take the second left turning to the Esplande. The swimming baths will be on your right."



You will ne	eed a copy of the Nottingham City Bus Services Route Map.
I. ■ Open u	p the map.
Right a	t the bottom you will find 'Farnborough Road' (in square B4).
 Now fir 	d the roundabout which joins 'Southchurch Drive' to 'Farnborough Road'.
 You sho starts h 	ould now be able to see a blue '53' in a red box (this red box shows that bus numbe ere).
	at this terminus, trace the route of the 53 bus as it goes round Nottingham. As you ake a list showing all the roads it travels along. Use the space below.
Number	53 bus route
Corner o	f Farnborough and Southchurch Drive
	with Drive
	rough Road (again!)
Fambo Clifton	hat your aunt lives on Wollaton Vale, near Balloon Wood (A2). She has to go to
Fambo Clifton	rough Road (again!)
Fambo Clifton . Suppose t University	hat your aunt lives on Wollaton Vale, near Balloon Wood (A2). She has to go to
Fambo Clifton 2. Suppose t University Which bus	hat your aunt lives on Wollaton Vale, near Balloon Wood (A2). She has to go to Hospital (B3) for a check-up.
Fambo Clifton 2. Suppose t University Which bus	rough Road (again!) Lane hat your aunt lives on Wollaton Vale, near Balloon Wood (A2). She has to go to Hospital (B3) for a check-up. could she catch?
Fambo Clifton 2. Suppose t University Which bus	rough Road (again!) Lane hat your aunt lives on Wollaton Vale, near Balloon Wood (A2). She has to go to Hospital (B3) for a check-up. could she catch?

Solution to question 1

Clifton Boulevard, Middleton Boulevard, Western Boulevard, Valley Road, Mansfield Road, Nottingham Road, Gedling Road, Rolleston Drive, Howbeck Drive, Killisick Road, Coppice Road.

Solution to question 2

Bus number 35. Wollaton Vale, turn left along Derby Road past Wollaton Park to the University Hospital.

STAGE 3 ASSESSMENT TASK 5

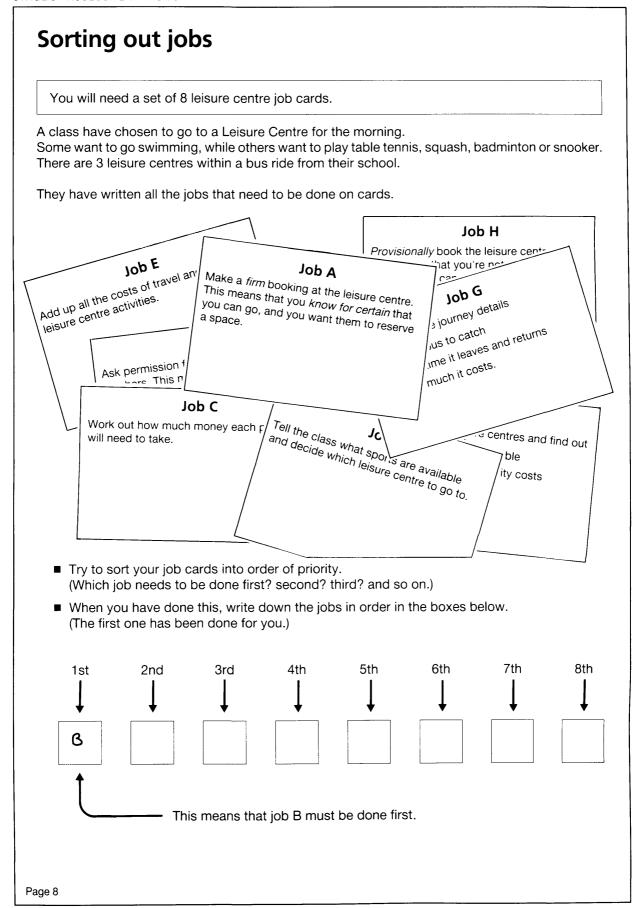
Asking for permission Imagine that your class is going on a trip to your local swimming baths next Tuesday morning. One person has volunteered to write a letter to parents, asking for permission: Dear Parent, We are going to the swimming baths next Tuesday. If _____ can go, please tick the box. Reply slip (Tear off and return to school) I agree that he/she can go. Make a list of all the important details that have been missed out of the letter.

Page 7

M31

A discussion of this task appears on page T81.

STAGE 3 ASSESSMENT TASK 6



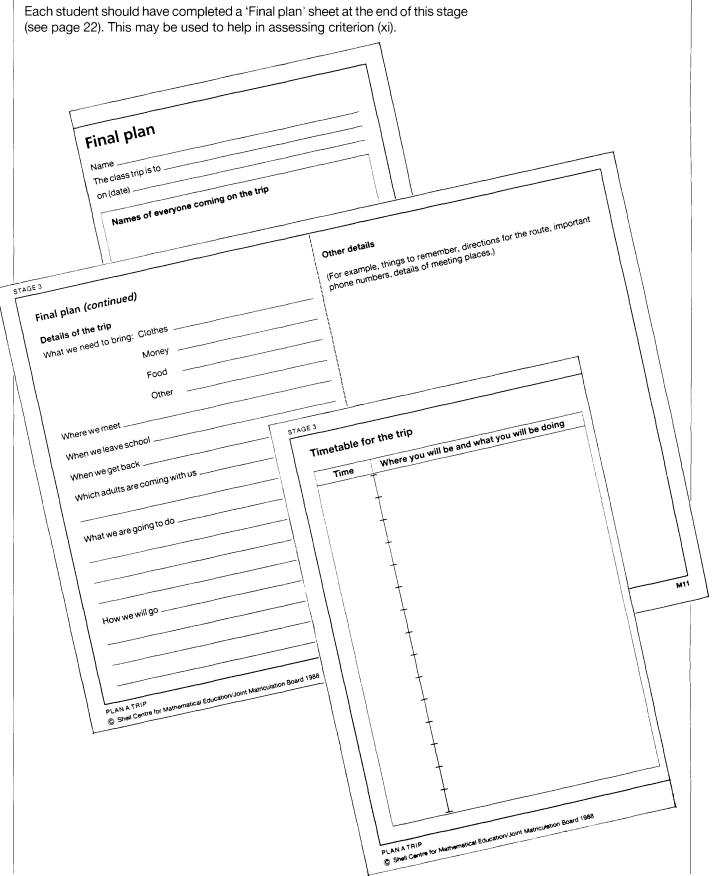
A discussion of this task appears on page T83.

STAGE 3

t out these 8 leisure centre job cards and us	
Job A	Job E
Make a <i>firm</i> booking at the leisure centre. This means that you <i>know for certain</i> that you can go, and you want them to reserve a space.	Add up all the costs of travel and leisure centre activities.
Job B Phone up the 3 leisure centres and find out what sports are available how much each activity costs when it is open.	Job F Tell the class what sports are available and decide which leisure centre to go to
Job C Work out how much money each person will need to take.	Job G Find out all the journey details which bus to catch what time it leaves and returns how much it costs.
Job D	Jop H
Ask permission from parents and teachers. This means telling them <i>all</i> the plans in detail.	<i>Provisionally</i> book the leisure centre. This means that you're not absolutely sure that you can go, but you want them to reserve a space for a while.

Stage 3 Assessment task 7

The 'Final plan' sheet



Stage 4 Going on your trip and evaluating it

Introduction

In this final stage, the trip takes place and then students compare what actually happens with what they had anticipated would happen. They are then asked to suggest ways in which the planning and running of the trip might have been improved.

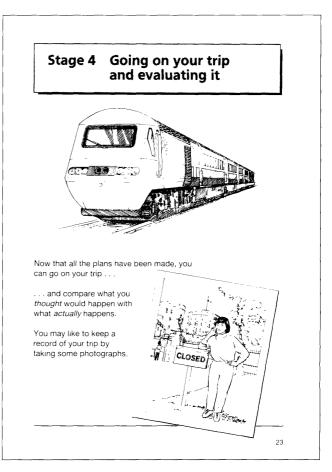
Total time needed

The evaluation should occupy between $\frac{1}{2}$ and 1 hour.

Organisation and equipment required

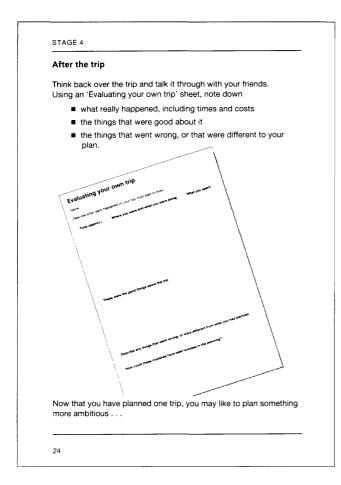
The class is responsible for the organisation and equipment for the actual trip.

For the evaluation each student will need a copy of an 'Evaluating your own trip' sheet.



Related assessment criterion

This stage offers students the opportunity to show that they can (xiii) evaluate the plan which has been implemented.



During the trip, it would be useful if some students could record what happens, perhaps by taking photographs and recording the times at which these were taken. This will facilitate a more accurate evaluation.

After the trip, students should be asked to analyse the differences between the actual trip and their plan. In particular, they should try to remember costs and approximate times when events occurred. (Perhaps someone could make a poster with the photographs that were taken – arranging them into sequential order and labelling them with times.)

It is important to be able to distinguish things that went wrong because of bad planning from those that were merely the result of unavoidable circumstances.

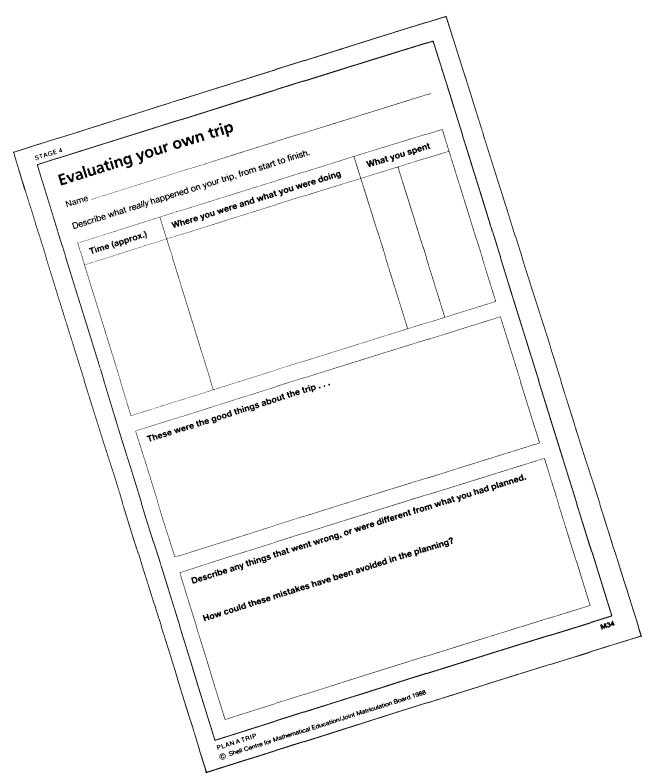
Assessment task for Stage 4

The 'Evaluating your own trip' sheet

The completion of this sheet will help you when deciding whether or not a student can

(xiii) evaluate the plan which has been implemented.

This task should have been completed within the normal course of the work.



Some possible further developments

The theme of 'Plan a Trip' leads naturally to development in many ways.

- Students may now enjoy the challenge of planning more ambitious trips. These may be trips which they intend to go on (e.g. the youth hostelling holiday mentioned in the interview on page T95), or which are imaginary but intriguing (e.g. a trip around the world or a comparison between a holiday to Great Yarmouth and a holiday to Ibiza (see below)).
- The planning experience gained may motivate a number of projects associated with the trip context (e.g. the organisation of a sponsored walk or the preparation of local youth-centred tourist information (see below)).
- Students may wish to transfer and develop their planning skills to a new context (e.g. the planning and running of a party or disco).
- You, or the students, may wish to use the module theme as a starting point for more involved problems or investigations, encouraging the development of mathematical techniques. This is explored in Chapter 3.

Three of these ideas are now discussed in a little more detail.

Comparing two holidays

Three friends and their parents are involved in trying to choose between a 10-day caravan holiday in Great Yarmouth and a cheap 10-day package holiday to Ibiza. Obtain some holiday brochures and help them to make an informed decision. Estimate the total cost of the holidays. (Include entertainment, clothes and food etc. as well as travel and accommodation costs.)

Often, mathematical problems associated with holiday travel concentrate solely on the costs of travel and accommodation, but there are many other costs associated with holidays. If these are excluded from any calculations (because, for example, they cannot be determined exactly) then the solution may become unrealistic. (When this problem was tackled by three students they were surprised to discover that the costs of the two holidays were not as different as had been anticipated!)

Organising a sponsored walk

Suppose that you decide to raise money for charity by organising a sponsored walk in your area.

Plan how you would do this and, if possible, put your plan into action.

Organising such an event requires many of the skills already used in 'Plan a Trip'. In addition, aspects of the problem which a group will probably need to consider include

- (a) agreeing on the objectives of the walk,
- (b) deciding on and maintaining effective organisation,
- (c) maximising income,
- (d) maintaining safety,

- (e) selecting and testing a suitable route,
- (f) estimating all the costs involved,
- (g) following any rules and regulations.

Job (a) might well involve a survey among possible participants, whilst (b) will call upon the listing and sequencing skills used in Stage 3. The total income obtained (c) is likely to depend on the average participants' cash collection from sponsors, the number of participants, and the organising costs (f). In turn, the cash collections are likely to depend on a variety of factors, including the perceived 'worth' of the cause, the motivation of the participants, the effectiveness of advertising and enlisting of participants, as well as the location and timing of the event. Often, events which are very demanding (and only open to a few participants), or which are seen as trivial (and unattractive to potential donors), are less profitable than those which require a modest achievement from a fairly large number of participants. The selection and testing of a suitable route and the location of checkpoints to fit agreed time and safety constraints, require the ability to make reasonable estimates of time and speed, as well as the ability to interpret maps.

Preparing a local tourist leaflet

Devise and produce a tourist leaflet for your town which is aimed at the teenage visitor. This will involve finding out and then displaying a variety of local information, including

- bus services, (different firms, times, route maps, fares)
- walking distances and times
- details of main attractions in the area
- suggested excursions, tourist trails etc.

Your group will then have to agree on how best to display the information from the visitor's point of view.

Find a way of mass-producing your leaflet. You may like to use a typewriter, word processor, or even a local printer. (Estimate the costs of this.)

This task may include

- conducting a survey to ascertain what are seen as the main attractions of the area and the kind of information that would prove particularly useful to a teenager
- producing a scale map of a local area, maybe using an Ordnance Survey map as a basis
- calculating costs, distances and travel times
- the utilisation of photographic, graphic and other art skills. (Perhaps this could involve the collaboration of teachers from other departments.)

Developing the mathematics

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Developing the mathematics

Introduction

While students are working on this module, their main objective is to devise a well-organised and interesting trip – not to develop particular mathematical techniques. You may, however, wish to use the opportunities provided by the module to motivate the learning of mathematics in a more explicit way. This chapter offers a few ideas on how this may be achieved without destroying the essential flow of activities contained in the module.

Which skills may be developed?

The table below illustrates a few of the mathematical topics that can be related to the context of this module. This list is not intended to be exhaustive because different trips will require different techniques in their planning. An afternoon trip to the local leisure centre will make different mathematical demands on students than, say, a day trip to France.

Some mathematical topics	Examples in the context of the module
Money	
 Carrying out simple monetary transactions in theory and practice 	Calculations carried out in 'The Matlock Bath Game', or during the trip itself.
Estimating costs.	Producing a rough costing for a proposed trip on the 'Ideas leaflet'.
Time	
 Understanding and using both 12 and 24-hour clocks. 	Reading bus and train timetables.
Producing a schedule.	Drawing up a timetable for the day of the trip on the 'Final plan' sheet.
Measurement	
 Understanding and using everyday measures of distance, time and speed. 	Using maps to calculate journey times.
Percentages	
 Understanding simple discounts expressed as percentages. 	Railcard discounts, and other party discounts are often expressed in this way.
Graphical and other representations	
 Extracting information presented in written, tabular or diagrammatic form. 	Using tourist information leaflets, timetables, route maps etc.
 Organising systematically the collection and presentation of data. 	Organising a 'Jobs schedule', filling in 'Job done' cards and reporting back to the class.
Logic	
Inventing and following a set of instructions.	Completing and using the 'Final plan' sheet.
 Arranging tasks into a logical order. 	Sorting out 'Job cards' into order of priority. Coordinating the completion of the jobs.
Statistics	
 Conducting a simple survey and making decisions based on the outcome. 	Devising a voting system and using it to decide on a suitable destination for the trip.

How and when may they be introduced?

Mathematical activity may be initiated either by the student or by the teacher. For example:

- A group of students may become aware of its need to acquire a particular skill in order to carry through its own plan. 'How do you use this timetable, Miss?'
- You may wish to use a part of the module to support a more intensive piece of work on a particular topic. 'Today we are going to look at voting systems. Can you remember how you voted on the best place to go for your trip?'

The first type of situation can lead to an invaluable learning experience because the student wants to know something. Such opportunities occur rather unpredictably, however, and it is inadvisable to spend a great deal of time helping one group if you have a large class to supervise. One possible solution is to ask a member of the group to describe the group's problem to the whole class and invite help and advice from other students. Another possibility is to use existing material to help develop some simple 'How to . . .' sheets. For example, the few pages at the beginning of the British Rail Timetable give a full explanation of how to read train timetables. If this presentation proves too difficult, a simplified version could be developed for classroom use.

Do not expect students to use, autonomously, mathematics that they have only recently been taught. There is a gap, typically of several years, between first 'learning' a skill and being able to use it with flexibility and fluency. Students will tend only to use skills that they have mastered. Narrowing this gap requires a more 'rounded' approach to learning, with a variety of applications and non-routine problem solving to supplement and give meaning to technical exercises.

Teacher-initiated work on mathematical techniques relating to the theme may occur *before*, *during*, or *after* working on the module.

Before: 'I'll do some work on ratio now, and then my class will be able to use the map scales later on, when they start work on the module.'

This timing has the advantage that the student will, if all goes well, have their techniques polished and ready to be used, but it does seem artificial to learn a new technique before seeing a need for it. Students may tend to assume that the module is merely a vehicle for practising some specific techniques, rather than to develop their autonomy in problem solving. *During:* 'They seem to be having some difficulty in interpreting the 24-hour clock. We'll take a break from the module for a few lessons and practise this skill.'

'I'll prepare some problems sheets for my class so that I can keep them together. So if one group finishes a stage early, they can do problem sheets until the rest of the class have caught up'.

This timing enables you to respond to needs as they arise, but if students always expect you to produce the method or solution when the going gets difficult, you may reinforce dependence and undermine autonomy. If this is done too often on a class basis then the work on the module may tend to drag on over many weeks and becoming boring.

After: 'When we finish the module, we will look at the techniques we have used in more depth.'

The experience of working on the module may motivate and enable students to perceive the value of techniques when they are taught. Students may still not be able to use techniques autonomously unless they are given further opportunities to apply them in real problem solving contexts.

Whatever you decide, it is important to be vigilant about preserving the students' strategic control of their work on the module; it is too easy to allow them to revert to the imitative roles that the traditional curriculum encourages.

On the following pages we offer a few ideas for developing mathematical tasks on the 'Plan a Trip' theme. We have not included examples which are already adequately covered in many textbooks (for example, using timetables, maps, and holiday brochures.) In their present form, the following ideas may be too open or too difficult for some students and may need some further development before you can use them. We hope that they stimulate some more ideas of your own.

Some sample ideas

Voting systems

Ten people are trying to decide where to go for a day out. They have four destinations to choose from: a castle, a theme park, a zoo and a museum. To begin with, each person ranks the 4 places in order of preference:

	John	Sue	Malcolm	Barbara	Rajiv	Hugh	Jenny	Judith	Rosemary	Alan
Castle	1	2	2	2	3	2	1	4	3	4
Theme Park	4	4	1	4	4	1	3	3	1	1
Zoo	2	1	4	1	2	4	4	1	2	2
Museum	3	3	3	3	1	3	2	2	4	3

(Thus, Sue has put down the museum as her third choice, and so on.) Where should they go? How do you decide?

At the end of Stage 2, students may experience difficulties in reaching an agreed decision on a destination for their trip and it may therefore be worth spending time in the discussion of decision-making processes.

One approach is to study the effects of different voting procedures on outcomes given the same input data. Students could be asked to suggest possible methods. The following are examples.

- Choose the place with the most first choices.
- Choose the place with the fewest fourth choices.
- Add up the rankings and choose the place with the lowest total.
- Eliminate the place with the fewest first choices, then ask everyone to vote again on the remaining destinations. Repeat this process until there is only one place left.

(It is interesting to note that, with the above data, the first three of these methods result in different decisions while the fourth remains inconclusive.) Students could also be asked to

- construct arguments for *choosing* each of the four alternative places
- construct arguments for *rejecting* each of the four alternative places

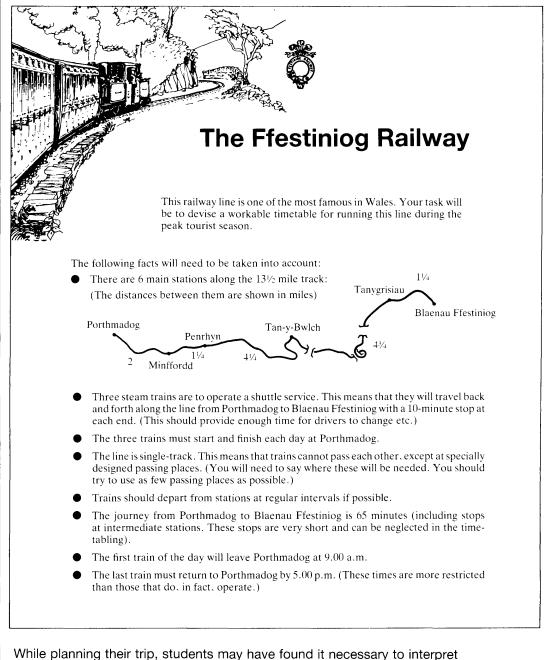
suppose that the people were able to run *two* of the four trips.

One method for choosing is to add the rankings and choose the two places with the two lowest totals.

(This process results in a very poor decision being made. What goes wrong? Which two places should have been chosen? Why?)

Further extensions are possible with this theme. General elections may be explored, together with issues such as proportional representation.

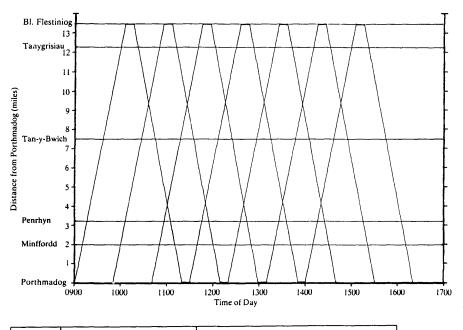
Timetables



While planning their trip, students may have found it necessary to interpret several bus and train timetables. They may have wondered how such timetables are constructed and some may enjoy the considerable challenge of inventing a timetable for themselves. Often, a graphical solution is the quickest and most accessible. For the above problem, for example, a student could begin by drawing a distance-time graph for the 9.00 a.m. train leaving Porthmadog, accurately showing

- the outward journey from Porthmadog to Blaenau Ffestiniog
- the waiting time at Blaenau Ffestiniog
- the return journey from Blaenau Ffestiniog to Porthmadog
- the waiting time at Porthmadog . . . and so on.

The other two trains may then be regularly spaced between successive departure times for this train. This will result in the following graph, from which a timetable may be constructed.



Miles	Station Daily Timetable								
0	Porthmadog	d	09:00	09.50	10.40	11.30	12.20	13.10	14.00
2	Minffordd	d	09.10	10.00	10.50	11.40	12.30	13.20	14.10
31/4	Penrhyn	d	09.15	10.05	10.55	11.45	12.35	13.25	14.15
71/2	Tan-y-Bwlch	d	09.35	10.25	11.15	12.05	12.55	13.45	14.35
121/4	Tanygrisiau	d	10.00	10.50	11.40	12.30	13.20	14.10	15.00
131/2	Blaenau Ffestiniog	a	10.05	10.55	11.45	12.35	13.25	14.15	15.05
0	Blaenau Ffestiniog	d	10.15	11.05	11.55	12.45	13.35	14.25	15.15
11/4	Tanygrisiau	d	10.20	11.10	12.00	12.50	13.40	14.30	15.20
6	Tan-y-Bwlch	d	10.45	11.35	12.25	13.15	14.05	14.55	15.45
10¼	Penrhyn	d	11.05	11.55	12.45	13.35	14.25	15.15	16.05
111/2	Minffordd	d	11.10	12.00	12.50	13.40	14.30	15.20	16.10
131/2	Porthmadog	а	11.20	12.10	13.00	13.50	14.40	15.30	16:20

(It is also worth noting that two passing places are needed, approximately 4.2 and 9.4 miles from Porthmadog.)

It is interesting to compare the timetable produced in this way with a real one, an extract of which is given below.

Porthmadog	d.	0840	0950	1035	1125	1220	1310	1400	1455	1545	1635	1900
British Ran Pwilhell Cambrian Coast kne Minffordo		0755	-	0938 1008		1135			1400 1433	1500		1640
NO SUNDAY SERVICE			0817 0901		0955 1040		1155		1343 1422		1520	1752 1834
Minffordd	d.	0849	0959	1044	1134	1229	1319	1409	1504	1554	1644	1909
Penrhyn	d.	"Early	1005	1050	1140	1235	1325	1415	1510	1600	1650	1915
Tan-y-Bwich	d.	Bird"	1025	1112	1205	1255	1345	1435	1530	1620	1710	1935
	d.		1043	1135	1223	1313	1407	1458	1548	1641	1728	1953
BI. Ffestiniog	а.	0940	1055	1146	1233	1325	1417	1507	1600	1652	1740	200
BI Flestiniog British Ra Liandudho Jo onwy valey line Liandudho	d n s	0945 1042 1055	1105 1204 1214			1330 1431 1441	1450 1548 1558		1625 1726 1736		1748 1845 1903	2020 2117 2127
NO SUNDAY SERVICE Bi Flestiniog	d. nd a.	0830 0840 0940	0950 1000 1100		1110 1121 1224			1333 1343 1445	1450 1501 1609		1630 1640 1741	1745 1803 1903
Bl. Ffestiniog	d .	1015	1105	1155	1245	1340	1430	1520	1615	1700	1746	201
Tanygrisiau	d.	1021	1111	1201	1251	1346	1436	1526	1621	1706	1752	202
Tan-y-Bwich	d.	1045	1133	1225	1315	1405	1500	1550	1640	1730	1814	2043
	d.	1101	1149	1245	1335	1424	1520	1606	1659	1746	1830	205
Minffordd	d.	1106	1154	1250	1340	1429	1525	1611	1706	1751	1835	2104
amouan Coast the Barmouth	đ		1205		1433	1530 1616		1710			1955	
See sales below Mintfordd NO SUNDAN SERVICE Pwilheil			1237 1305		1422		1606 1633			1834 1901		2212 2239
Porthmadog	9	1120	1200	1304	1354	1444	1539	1629	1719	1805	1848	011

Networks

The 'Tour of Britain' project

You will need a copy of the AA Members Handbook, or a similar resource, which gives details of accommodation, mileage charts and maps.

Imagine that you own a coach company in your home town, and that it is your job to organise a one week coach tour of Britain, visiting at least 7 of the towns shown on the map.

Choose the towns that you think would appeal to foreign tourists.

Sketch a network showing the distances between these towns and find the shortest route by which you could visit each of them and return home.

Estimate how long each of your journeys will take (assuming an average speed of 40 mph) and draw up a rough timetable for the tour. Allow plenty of time for sightseeing.

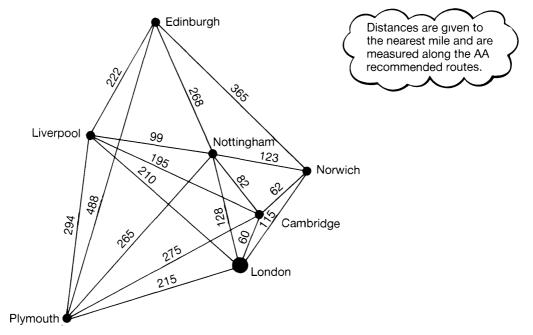
Choose your overnight stops, and try to find reasonable but cheap accommodation. Make estimates of the driver's wages, petrol costs and other expenses. Calculate the cost per passenger (assume there are 50 tourists) which would enable you to 'break even'.

Produce a brochure advertising the tour.



This project idea begins with an open-ended version of the 'Travelling Salesman' problem. Suppose that the coach firm is based at London, and that the 7 towns selected are London, Plymouth, Edinburgh, Nottingham, Liverpool, Cambridge and Norwich.

The network which results is shown below.



No general algorithm for finding the minimum distance around such networks is known, apart from enumerating all the possible routes. (In this case,

however, this is not too difficult.) If there are n towns, there are at most $\frac{(n-1)!}{2}$

possible routes, and for even moderate values of n this number of possibilities is too large to handle on the most powerful computers*.

The remaining activities may be made as realistic as the student wishes. Additional data, such as the fuel consumption of a coach, may either be estimated or researched via a few letters or telephone calls. The final report may prove suitable for assessment as GCSE coursework.

Shopping

You arrive by bus in the centre of a nearby town at 10 o'clock and have to catch a bus from the bus station at 11.30.

You've noted down what you want to do in the time.

buy pair of shoes buy tickets for rock concert buy cookery book (present for Jane - her birthday tomorrow) and post it get more cash from Building Society - (only got £20 now) meet Julie at bus station at 11.30 get stamps get wrapping paper and card

Plan the best route and timetable you can, to carry out these tasks. Make sure you allow reasonable time for walking from place to place as well as for shopping.

Your students will need a scale map of a real or fictitious town centre, showing a variety of shops and other locations.

You will be able to devise a range of problems of a similar sort, using the same map.

Your students may also enjoy making up such problems and giving them to each other to solve.

* (Students may like to compete against a computer in finding the shortest route around 10 towns of their choice, using the program SALESMAN. See, Teaching with a Micro, Maths 1, Shell Centre for Mathematical Education, University of Nottingham 1984. ISBN 0 906 126 223.)

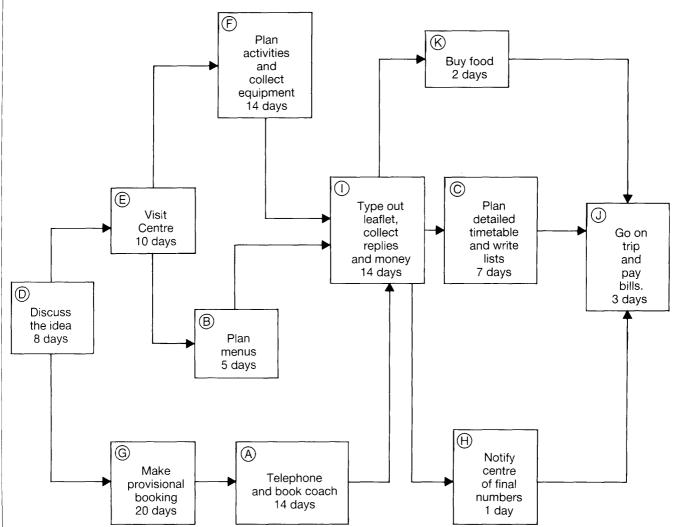
Critical path analysis

Six teenagers are planning a weekend trip, starting on May 30th, to a youth centre for their youth club. They have made the following list of essential jobs, together with approximate times, within which each job should be done.

dof	Time allowed
Telephone a few coach firms, get quotes, choose the best and confirm the booking in writing. Wait for and receive a reply.	14 days
B) Plan the menus.	5 days
Work out a detailed timetable for the weekend and write out dormitory lists, washing up rotas and so on.	7 days
Discuss the idea of the weekend with the youth club members and get a rough idea of the number interested in going.	8 days
Go and visit the Centre to check on the facilities (for activities, cooking, sleeping etc) that are offered.	10 days
Plan the various activities that will take place and collect together all the necessary items of equipment.	14 days
Make a provisional booking for the Centre, pay a deposit and receive confirmation.	20 days
Notify the Centre of the final numbers that are going.	1 day
) Type out an information leaflet about the weekend (including dates, times, travel details, costs, planned activities and a description of the place). Issue the leaflet to the youth club members, collect replies and the money.	14 days
) Go on the trip and pay all outstanding bills.	3 days
) Buy food.	2 days

Draw a network to show a logical order for doing these jobs. (Remember that some of the jobs can be done at the same time by different people.) Find out the minimum time that will be needed for doing all the jobs, and the latest day by which each job must be finished.

Although we have given this problem the rather daunting title of 'Critical path analysis' it should not be assumed that students need a formal knowledge of this subject before they can attempt to solve the problem. Each job could be written as a card and the cards rearranged physically, thus enabling an interesting and worthwhile group discussion to take place. A possible solution is shown below.



The minimum time for completing the jobs is thus 66 days. Working backwards along the network, each job may now be given a date by which it must be completed.

The above technique has many applications in industry and commerce. Students may enjoy the challenge of using similar techniques to plan one of the following projects.

- Moving house.
- Putting on the school play.
- Building a house (or a doll's house).
- Cooking Sunday Lunch.
- Decorating a room.

(For further discussion of critical path analysis see, for example, 'Decision Mathematics' by the Spode Group, Oxford International Assessment Services Ltd and Ellis Horwood Ltd 1986 ISBN 0-7458-0078-5.)

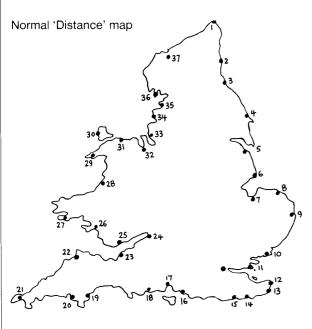
Maps

On a map you can usually tell how far away a place is, and in which direction you should travel to get there, but you cannot tell how long your journey will take nor how much it will cost. Here is one method for drawing a 'train times map' measured from your town.

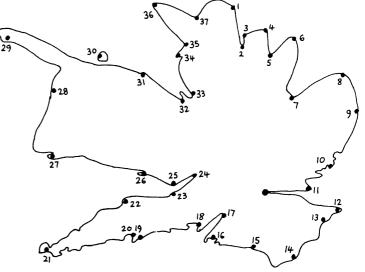
- Using an atlas trace the positions of your town and some major cities and coastal towns onto a sheet of paper.
- From a timetable, find out the shortest time it will take you to get from home to each of these places.
- Using a suitable scale (e.g. 2 cm represents 1 hour) 'move' the towns and cities directly towards or away from your town (keeping the same bearing), until their positions correspond to the journey times.
- Sketch in a 'coastline' of Britain through the new positions of your coastal towns.
- Add as many further details to your map as you feel necessary.

Compare your map with a similar one showing train fares. Which routes are the best value for money?

This activity produces a topological distortion, like the one drawn below, which illustrates travel times from London.



'Times from London' map



Number	Place	Time	Number	Place	Time
1	Berwick-upon-Tweed	4h 3m	20	Plymouth	3h
2	Newcastle-upon-Tyne	3h 10m	21	Penzance	4h 52m
3	Hartlepool	3h 26m	22	Barnstaple	3h 3m
4	Scarborough	3h 32m	23	Weston-Super-Mare	2h
5	Grimsby	2h 53m	24	Gloucester	1h 33m
6	Skegness	3h 25m	25	Cardiff	2h
7	Kings Lynn	2h 5m	26	Swansea	2h 40m
8	Cromer	3h 2m	27	Pembroke	4h 41m
9	Great Yarmouth	2h 40m	28	Aberystwyth	5h 5m
10	Clacton	1h 30m	29	Pwllheli	6h 30m
11	Southend	0h 55m	30	Holyhead	4h 40m
12	Margate	1h 37m	31	Colwyn Bay	3h 40m
13	Dover	1h 23m	32	Chester	2h 40m
14	Hastings	1h 30m	33	Liverpool	2h 41m
15	Brighton	1h 10m	34	Blackpool	3h 32m
16	Portsmouth	1h 30m	35	Morecambe	3h 36m
17	Southampton	1h 3m	36	Barrow	4h 44m
18	Bournemouth	1h 38m	37	Carlisle	4h
19	Torquay	2h 58m			

Students may like to draw similar time maps for bus or undergound train networks for their own localities.

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Optimisation

Where do you locate your headquarters?

A new national organisation concerned with life in the countryside was recently faced with the problem of where to locate its headquarters. Staff would be required to travel to branches throughout England and to return, if possible, on the same day either by car or train. Branch representatives would need to be able to travel, usually by train to the headquarters for meetings, also returning home on the same day.

An analysis of train times was carried out for a selection of possible locations (see below).

- Investigate the suitability of each different location, using further data as well as that given.
- Try to select the two best locations, giving reasons for your choices.

You may find maps and mileage charts provided by the AA or RAC of use. A reasonable assumption for speeds is that cars can travel at an average speed (including stops) of 60mph on motorways and 40mph on other roads.

		Br	Branch locations																										
	to from	London				Birmingham				Newcastle			Carlisle				Norwich				Southampton				Plymouth				
ers		а	d	f	t	а	d	f	t	a	d	f	t	a	d	f	t	a	d	f	t	а	d	f	t	а	d	f	t
Possible location of headquarters	Cheltenham	0830	2100	13	21/4	0800	2230	12	1	1200	1900	9	4	1200	1800	6	6	1200	1800	6	6	1000	1830	8	3	1000	1930	8	3
	Rugby	0800	2130	23	1	0630	2300	20	3/4	1130	1700	7	4½	1100	1730	6	51/2	1030	1800	8	5	0830	2100	12	21/2	1230	1900	10	57
on of	Stafford	0930	2030	23	1	0700	2130	28	3/4	1130	1800	12	5	0900	2000	10	3	1030	1700	7	43⁄4	1030	1830	12	4	1130	1800	6	43/
ocatio	Leicester	0830	2200	30	11⁄4	0700	2200	14	1½	1030	1830	7	3¾	1030	1830	8	4	0930	1930	7	3	1030	1930	10	3½	1230	1730	6	5%
	Peterborough	0630	2230	32	1	0800	2030	11	21⁄4	0800	2100	20	21/2	1230	1900	8	4½	0800	2100	9	2	0930	1900	20	3	1130	1830	8	51/2
Possi	Derby	0930	2130	19	13⁄4	0730	2100	20	3/4	0930	1930	9	3	1100	1800	8	5	1100	1800	7	31/2	1100	1830	10	4	1130	1730	8	41/2

a earliest arrival time (approx)

d latest departure time to return to base by midnight (approx)

f number of trains per day in each direction

t average journey time in hours

At the time of writing, the organisation (ACRE) has yet to decide on the permanent location for its headquarters, but appears to have rejected Peterborough (which might seem to be a good choice) for somewhere between Cheltenham and Swindon. The actual analysis involved the consideration of 9 further locations in addition to the 6 shown here.

There were many other factors not directly concerned with travel which had to be taken into account. For instance, the personal preferences of key staff, the existence of suitable property for rental and other housing considerations.

Maybe this illustrates that mathematical analysis often serves to clarify issues, but that ultimate decisions may depend on human non-mathematical considerations. However the analysis certainly helped to indicate where *not* to locate the headquarters. Possible areas such as Salisbury, Sheffield, Lincoln and Preston were all rejected in the early stages.

(These figures were obtained from a 1986 British Rail timetable)

The role of assessment

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The role of assessment

Introduction

Why assess?

You may wish to assess your students' work for a variety of reasons. The style of assessment you use should reflect the purpose it has to fulfil. For example, you may be using the module in the context of an assessment scheme (e.g. the JMB Certificate of Numeracy through Problem Solving, GCSE coursework or Records of Achievement), or you may simply want to assess school work, to enable you and your students to recognise their progress.

The purpose will affect the aspects of your students' work that you decide to assess. These include (with examples)

- strategic skills (the ability to plan and organise)
- technical skills (the ability to read timetables accurately)
- social skills (the ability to take account of other peoples' viewpoints).

Each of these poses a distinct assessment challenge.

In this chapter, we will focus on ways of assessing and recording

- a student's work within a group setting
- the strategic and technical skills deployed, as referred to in the Introduction (pages T5 and T6).

We include illustrations of students' work based on the assessment tasks which are associated with each of the four module stages. In addition, we offer examples of two 'examination papers' for students of different ability levels. These papers may be used to help assess your students' retention of skills and their ability to transfer them to unfamiliar situations within the same context. In designing these assessment tasks we have sought to ensure their *curriculum validity*; i.e. that each task should also represent a valuable learning activity.

Assessing a student's work within a group setting

The theme of the module encourages group work, developing each student's ability to discuss, listen and cooperate with his or her colleagues. Such group work will often result in better planning than individual students could produce in isolation. Your observation of the groups at work will enable you to note some of the social skills which a student displays. Such skills include

- persistence and attention to detail
- the ability to coordinate the work of the group
- initiative
- the ability to work well in a team
- the ability to communicate.

These skills are valuable and worth recording whenever you are aware that they are being displayed by a student. It is difficult, however, to assess students reliably in this context because their performances are likely to be affected by the nature of the input from other group members, and by how well individuals can cooperate. A student may take an active role in one group, but be overshadowed by a dominant personality in another. Merely observing the work of the group as a whole may not give a clear picture of an individual's contribution, acquisition of skills, or understanding of the work of the group.

Thus, you may also wish to carry out some form of individual assessment. Four possible methods are:

One-to-one discussion with an individual student, possibly using a checklist of some kind.

This method is time-consuming, particularly with larger classes, and it is difficult to carry out an interview if you are simultaneously trying to supervise the rest of the class.

Observation of individual students by the teacher.

When groups are working cooperatively, group members tend to adopt complementary roles. This means that you are unlikely to see every student carrying out every task. This becomes more pronounced when class tasks are shared out amongst groups.

Students completing a number of specific individual written assessment tasks at stages during the work which reflect their recent group activities.

This has the disadvantages that some skills cannot be assessed in this way, and some students have difficulty in expressing themselves fully in writing, leading to responses which fail to reflect their true abilities.

Students carrying out self-assessments, which describe those aspects of the group work where

they have made particular contributions. Such selfassessments may consist of written notes or the completion of a simple checklist.

A combination of these methods is likely to provide an optimum approach to assessment. Some written tasks may be used with follow-up interviews being carried out to clarify incomplete or confusing responses from individuals. Observation and self-assessment will provide further complementary information. With a class of very low attainers, where the numbers are often small, you may prefer to assess by using mainly oral methods.

Assessing with reference to criteria

The criteria listed below are restatements of the general strategic skills in the context of this module, and have been referred to throughout the classroom materials. Students are given the opportunity to show that they can, in the context of planning a trip,

- (i) evaluate a plan and identify faults in it (including expenditure of money and time),
- (ii) generate lists of alternatives,
- (iii) devise a satisfactory rough plan (including sensible costings and time schedules),
- (iv) use and describe a decision making process, obtain and interpret information from
 - (v) a telephone directory,
 - (vi) aural and written timetables,
 - (vii) a street map,
 - (viii) a route map,
- (ix) identify omissions in given information,
- (x) place given jobs in a logical order,
- (xi) complete a clear and comprehensive final plan,
- (xii) take an active part in the planning process,
- (xiii) evaluate the plan which has been implemented.

Such criteria assist in providing a useful profile of relative strengths and weaknesses. However, to say that a student has satisfied a criterion, such as 'can evaluate a plan and identify faults in it', has little absolute meaning without specifying

- the context. Evaluating a plan for a trip is very different from evaluating a plan for the building of a house.
- the complexity within the context. Planning a trip round the world is far more complex than planning a trip into a local town.
- the frequency of success. Has the student satisfied the criterion on many occasions or only once? What proportion of attempts resulted in success?

- the amount of help given. How much help did the student receive from the teacher or other group members in understanding and completing the task?
- the occasion. When did the student attempt the task? How recently had the student experienced a similar situation?
- the distance of transfer. How closely did the task match the student's previous experience?
- the mode of response. How did the student respond to the task – in writing or orally?

Thus, if you are basing an assessment on work undertaken on this module alone, you will need to qualify any statement about a student's performance with some additional remarks like 'these abilities have been demonstrated while the student took part in planning a class trip to a local destination'.

If however students work through a range of extended activities, perhaps corresponding to the range of modules in this series, they are likely to develop the ability to demonstrate similar strategic skills in a variety of different contexts. This will then enable you to make more general statements about a student's ability to satisfy particular criteria.

Recording students' achievements

You may find it helpful to record your students' successes on a grid like the one shown on page 75. The criteria associated with this particular module have been listed across the top, and there are spaces for students' names to be filled in down the side.

There are many ways of filling in the cells in this grid. You may wish to record only that a student has satisfied or 'passed' a criterion, or you may wish to qualify this by recording, for example, the amount of help that was given and the frequency of success. Thus,

- P may mean 'pass with no help'
- Ph may mean 'pass with a little help'
- PH may mean a 'pass with a lot of help'
- PP may mean that a student has 'passed' the criterion on more than one occasion.

You may also wish to record whether a criterion was satisfied by a written or by oral response. Note that these may be assessed either by individual tasks or during the normal class work. If a student has not yet shown that he or she can satisfy a criterion, we suggest that the cell should be left blank, and the student be given a further opportunity at a later date so that only positive achievement is recorded.

An alternative would be to use a numerical grading system on a 3- or 5-point scale. But there is always a temptation to add such numbers so that a single score is obtained for each student. Although such a result is convenient, it is meaningless and misses the whole point of criterion-referenced assessment.

You may wish to extend your record sheet to allow space for comments concerning the social skills that your students have displayed, together with any particularly noteworthy achievements.

Assessing technical skills

It is relatively easy to test specific technical skills by assessment tasks which are context-free or set in a context contrived to give an air of realism. However, technical skills only become of value in problem solving when they can be deployed readily in the solution of the problem. This requires a student to choose an appropriate technical skill which he or she is confident in using. Thus the technical skill is a means to an end rather than an end in itself.

For these reasons, we feel that if technical skills are to be assessed, this should be done in real problem solving contexts. You will find examples of this throughout the sample assessment scheme. For instance, the Stage 1 assessment task requires students to perform calculations with money and time within a situation with which they are already familiar.

	Stage 1		Stage 2	2	Stage 3									
Criteria satisfied A student has shown that he or she can:	evaluate a plan and identify faults in it (including expenditure of money and time)	generate lists of alternatives	devise a satisfactory rough plan (including sensible costings and time schedules)	(iv) use and describe a decision making process	obtain and interpret information from	(v) a telephone directory	(vi) aural and written timetables	(vii) a street map	(viii) a route map	(ix) identify omissions in given information	(x) place given jobs in a logical order	complete a clear and comprehensive final plan	(xii) take an active part in the planning process	i) evaluate the plan which has been mplemented.
lame	Ξ	(ii)	(iii)	(iv)		 				(ix)	×	(xi)	(xii	(iiiix)
							_							
							_							
							_							
						+	_	-+						

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Using the assessment tasks

We will now look at a selection of the assessment tasks in more detail. With each task we include

- the related assessment criteria
- examples of students' work to illustrate the type of response which might satisfy particular criteria
- suggestions on recording achievement, using the approach already described.

These 'satisfactory' responses indicate what we believe is achievable by a substantial majority of 13–16 year old students. You may wish to vary this standard, however, depending on the ability level of your students and the particular assessment approach you are adopting.

The tasks included here are:

Stage 2, Assessment task 2	'Ideas leaflet'
Stage 2, Assessment task 3	'The vote'
Stage 3, Assessment task 5	'Asking for permission'
Stage 3, Assessment task 6	'Sorting out jobs'

Stage 2 Assessment task 2

'Ideas leaflet'

Ideas leaflet

STAGE 2

Time

Related criterion:

(iii) A student can devise a satisfactory rough plan including sensible costings and time schedules.

Required response

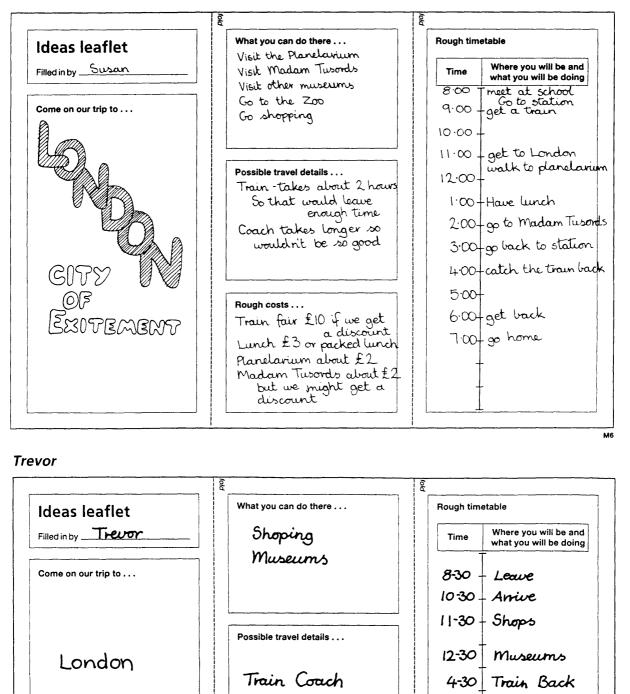
The 'Ideas leaflets' should give sufficient information for the class to make a decision. It should include

- the exact destination
- a description of possible activities
- some awareness of possible modes of transport and their feasibility in terms of time
- itemised, realistic costs
- a complete timetable showing realistic estimates and consistent with the rest of the information on the leaflet.

As the task is designed to show how well individuals have understood the work of the group, you should also take into account your observations of students' individual contributions.

Trevor and Susan, for example, are members of the same group. Susan's 'Ideas leaflet' shows that she has thought through the trip carefully and has made reasonable estimates about money and time, so she satisfies the criterion. Trevor, on the other hand, has failed to convey an adequately detailed description of what can be done in London, a sufficient number of travel details, or a realistic, itemised costing. The timetable is adequate, though brief. It may be that Trevor took a satisfactory part in the work of the group but has problems expressing himself in writing, in which case he needs to talk through the trip and write down the ideas as he says them.

Susan



Rough costs ...

£5

77

Mő

6-30 get back

STAGE 2 ASSESSMENT TASK 3 The vote Six people are planning a trip. Six different places have been suggested. a) The ice rink d) A castle b) Zoo e) Snooker hall c) Bowling alley f) Swimming pool In order to choose between these places, they decide to vote. Each person is given a list, and they write down their preferences. This is what they write: Sanjay John Claire a) Ice Rink 1st Choice a) Ice Rink 6th choice a) Ice Rink 6th choice b) ZOO 2nd Choice b) ZOO 5n choice b) Zoo lat choice c) Bowling 3rd choice d) Castle 2rd choice c) Bowling 5th Choice c) Bowling 1st choice d) Castle 4th Choice e) Snooker 3rd Choice d) Castle 2nd choice e) Snooker 4th choice e) Snooker 41 choice f) Swimming 5th choice f) Swimming 6" Chorce f) Swimming 3rd choice Jenny Elaine Mike a) Ice Rink 6m choice a) Ice Rink 4th choice a) Ice Rink 6th choice b) ZOO 3rd choice b) ZOO Gu choice b) ZOO 5m choice c) Bowling 5m choice c) Bowling 2nd choice c) Bowling 4m choice d) Castle 3rd choice d) Castle (st choice d) Castle 2nd choice e) Snooker 1st choice e) Snooker 4 th choice e) Snooker 3rd choice f) Swimming 2nd choice f) Swimming 5th choice f) Swimming 1st choice Which place would be the best choice for their trip? _ Explain how you get your answer:

Stage 2 Assessment task 3

Related criterion:

(iv) A student can use and describe a decision making process.

Required response

The best choice for the trip is the castle. This answer can be arrived at through a variety of different decision-making methods. For example

- adding the rankings gives (a) 29, (b) 22, (c) 20, (d) 14, (e) 19, (f) 22
- rejecting any option which is someone's 5th or 6th preference leads to (d) or (e), and of those (d) is clearly the better choice
- counting the number of 1st and 2nd preferences for each destination leads directly to (d).

If a different answer is reached, through a clearly described sensible process, the student also satisfies the criterion.

Wayne

Which place would be the best ch	noice for their trip? <u>Caste</u>
Explain how you get your answe	er:
Highest up most	choice de laste number is Lists
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	
a) The ice rink <b>29</b> b) Zoo <b>22</b> c) Bowling alley <b>20</b>	d) A castle <b>\4</b> e) Snooker hall <b>\9</b> f) Swimming pool <b>2.2</b>

Wayne has used the first method correctly, although the explanation is poor. He has satisfied the criterion.

#### Claire

Which place would be the best choice for their trip?									
Explain how you get your answer:									
because it is the best on the list the									
most populer is castle because it was									
most favourile									

Claire has not explained her method. She should be asked to explain how she reached her answer in order to satisfy the criterion.

#### Shazida

Which place would be the b	est choice for their trip?
Explain how you get your a	nswer:
give everyone	3 votes
ice rink 111	castle 1111
300 111	snooker III
bowling 111	swimming 111

Shazida has used a different method, giving each person's first three choices equal weighing. The method is clear so her response satisfies the criterion.

STAGE 3	ASSESSMENT	TASK 5
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## Asking for permission

Imagine that *your* class is going on a trip to *your* local swimming baths next Tuesday morning. One person has volunteered to write a letter to parents, asking for permission:

Dear Parent, We are going to the swimming boths next Tuesday.
If can go, please tick the box.
Reply slip (Tear off and return to school)
I agree that he/she can go.

Make a list of all the important details that have been missed out of the letter.

Page 7

#### Stage 3 Assessment task 5

#### **Related criterion:**

(ix) a student can identify omissions in given information.

#### **Required response**

Important details that have been missed out include

- money required
- member of staff responsible what people should bring
- time of departure

date of visit

- space for signature on reply slip
- time of return
- student's name on reply slip It is reasonable to expect that at least five points are mentioned, one of these

being the date. In the examples of work shown below, Philip is the only student who has not satisfied the criterion. Trudi has included the necessary details in her letter, showing an ability beyond that required by the task.

Andrew

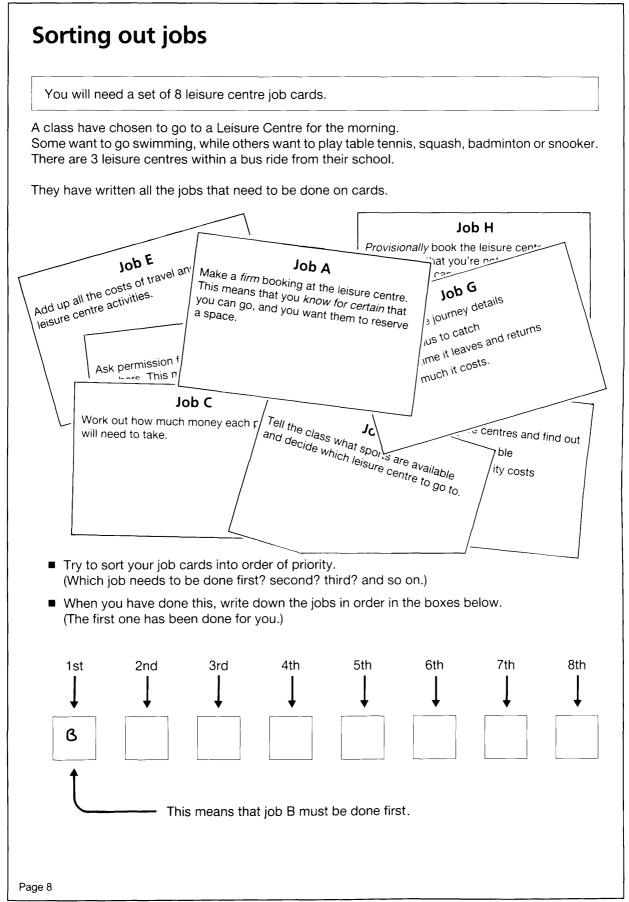
Nina

The DATE Who is Taketing Them THE TIMES OF DEPARTURE OND ATMULE IF IT GOSTS ANY Money Sighmed by He haucher	Name of Child. parent= Signed. Date Which Battis they are going to Do they NORED any Bustoir How they are getting their
Philip	what time they will return Home.
What time do we set OFF. How much will it cost, what time do we get back. What do we need as Sandwiches	teacherin charge. How long will they be their if they need on pook Lunch.

Trudi

Dear parent, We are going on a trip to Altringham Swimming baths on Tuesday 20th July. The head master has given us permission. IF ..... can go please tick the box. your child will need at last one pound fifty for entrance fees and bus fares plus his ther own food we will leave at 12.00 we will arrive home at 4.15. Signed

STAGE 3 ASSESSMENT TASK 6



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#### Stage 3 Assessment task 6

#### **Related criterion:**

(x) A student can place given jobs in a logical order.

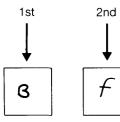
#### **Required response**

Several orders for the jobs are possible, but there are some sequences which must be preserved. В F

- Job F must come before job E.
- Job F before job H before job D before Job A.
- Job G before job E before job C before job D.

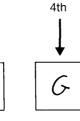
Other sequences are debatable, for instance whether job F should come before job G or not.

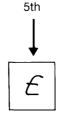
Azram

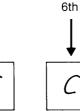


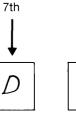


3rd









G

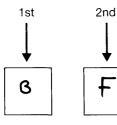
F



8th

Azram's order is well thought out so he satisfies the criterion.

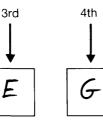
Azim

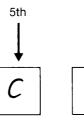


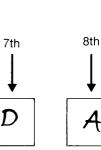
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2nd

C







Azim has got the 'GEC' sequence wrong, so he should be given the opportunity to think through the task again.

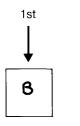
6th

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6th

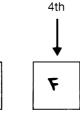
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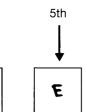
Lisa

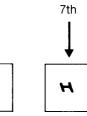


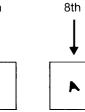
G

3rd









Lisa's sequence is unworkable and it is likely that she would benefit from further work in order to be able to satisfy the criterion.

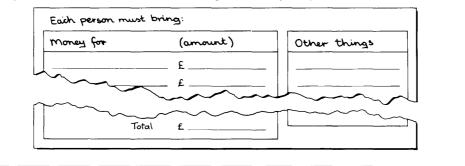
### Written examination papers

The two examination papers which follow may serve as a useful resource in assessing a student's ability to retain and transfer the skills to fresh situations in the same context.

Paper 1 is intended for nearly all students.

Paper 2 is intended for approximately the top 30% of students.

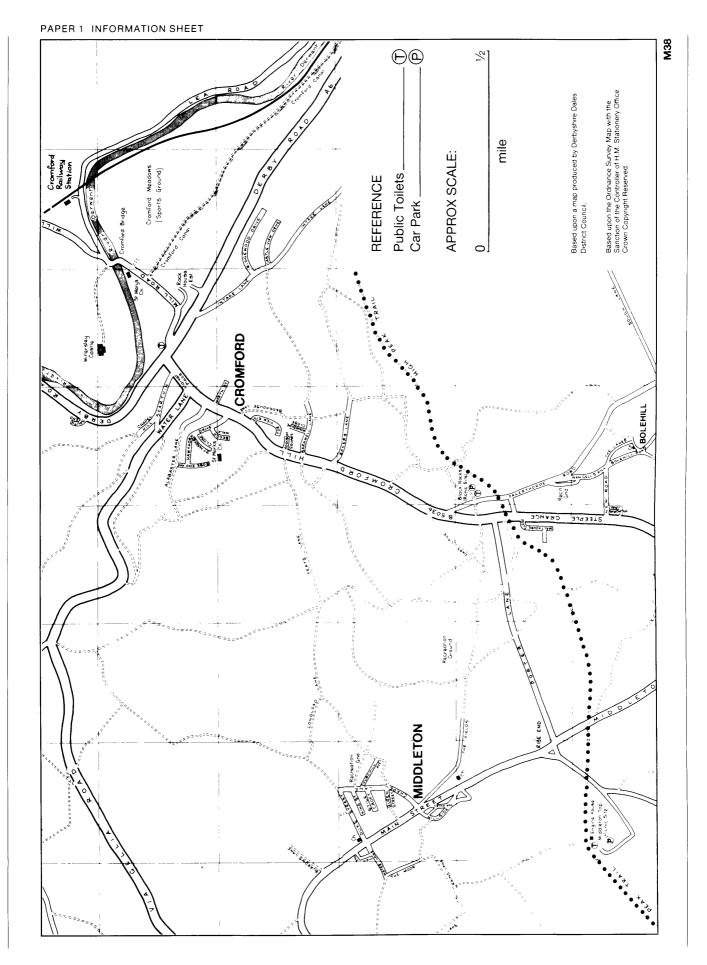
PAPER 1 A day out in Derbyshire You will need the information sheets M37, M38, M39 and M40. Alison and two of her friends live in Loughborough. They have planned a cycling trip around Derbyshire for Saturday 25 October. Alison's mum has offered to go with them if necessary, since all three girls are only 15 years of age. Unfortunately, the girls have made many mistakes and forgotten several things in their planning! 1. Read through their plan and the information sheets carefully. Whenever you find a mistake, or realise that something has been forgotten, write it down and say how they should change their plan The girls' plan Meet at Loughborough station at 7.23 a.m. Buy tickets and then catch the train to Derby. This arrives at 7.51 a.m. At Derby, catch the 8.20 a.m. train to Cromford. This arrives at 8.41 a.m. Here are the instructions for getting to the Cycle Hire Centre: "Turn left as you come out of Cromford station, walk along by the river, cross over Cromford bridge and walk down Mill road. Cross over the A6, and walk through Cromford. Keep going for about half a mile up Cromford hill and you should see Oakerthorpe road on your left. Walk up this a little way and you'll see the car park and picnic site where they hire out the bikes." Arrive at the cycle hire centre just before it opens at 9.30 a.m. Each person only needs £2 to hire a bike for the whole day. Cycle along the High Peak Trail, until it meets the A515. Then go through Monyash and along the B5055 into Bakewell - a total distance of about 15 miles. We'll allow 3 hours for the ride, so we should arrive in Bakewell by about 12.30 p.m. Spend about an hour in Bakewell, have a look round the shops, buy and eat our lunch. At 1.30 p.m. leave Bakewell and cycle over to Chatsworth House, where we'll spend 2 hours looking around the House, Garden and Adventure playground. At 4.00 p.m. leave Chatsworth and cycle down the B6012 and the A6, arriving at Matlock at about 4.30 p.m., where we'll look around the shops until 6.00 p.m. Ride the couple of miles back to Cromford, and catch the train that leaves at 19 minutes past 6. The train arrives at Derby at a quarter to 7. Wait around for the 7.58 p.m. train to Loughborough. This arrives at 8.14 p.m. 2. Alison and her friends eventually sort out their mistakes. Alison starts to make a list showing everything she must bring. Copy and complete her list. (Make sensible guesses at figures you don't know.)



#### PAPER 1 INFORMATION SHEET

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WRITTEN EXAMINATION PAPERS

#### PAPER 1 INFORMATION SHEET

Derbyshire



One of England's most beautiful and best-loved houses, in a splendid setting on the banks of the River Derwent in the Peak District National Park.

Chatsworth is famous the world over for its unrivalled private art collection, state apartments, and the Garden with cascade and fountains. The present House was built in 1678-1707 for the 1st Duke of Devonshire, with additions by Wyatville for the 6th Duke between 1820 and 1830.

#### A DAY AT CHATSWORTH

A visit to Chatsworth is much more than a visit to one of the most beautiful houses in Great Britain. There are plenty of things to see and do to interest all members of the family for a whole day.

Chatsworth House contains one of the finest collections in the world of paintings, furniture, tapestries, china, sculpture and gold and silver plate, collected by fifteen generations of Cavendishes. Visitors follow, at their own pace a clearly marked route round the House for which you should allow at least one hour.

The 105 acre garden is famous for its landscape, fountains and cascade. It is so big that there is always room to find peace and quiet. Dogs on leads are welcome.

Children find the Farmyard particularly interesting, especially the daily milking demonstration. The Adventure Playground, within the Farmyard, thrills and delights children of all ages.

#### **ADMISSION CHARGES**

#### House and Garden

£3.20
£2.50
£1.50
£2.50
£8.00

#### **Pre-booked Parties**

Adults	£2.75
Senior Citizens	£2.25
Students	£2.25
School Parties (including accompanying staff)	£1.50
Garden only	
Adults	£1.50
Children	£0.75
Farmyard and Adventure Playground	
Adults	£1.30
Children	£0.70
Family	£3.50
Scots Suite	
Adults	£0.30
Children	£0.15
Car Park	£0.50

#### **OPENING TIMES**

23rd March to 26th October, 1986	Opening times House Garden EVERY DAY 11.30-4.30 11.30-5.00
	Visitors are asked to conclude their visit to the House and Garden one hour after the above times.
Farmyard and Adventure Playground 23rd March to 21st September	EVERY DAY 10.30-4.30
Saturday & Sunday 30th & 31st August	House and Garden open to Country Fair visitors only.
Friday, Saturday & Sunday, 3rd, 4th & 5th October	House and Garden open to Horse Trial visitors only.



PAPER 2

### Trips on the Leeds – Settle – Carlisle railway

You will need to refer to the information sheets M44, M45 and M46 for this task.

Imagine that you were the organiser for two separate day trips due to leave from Keighley on Saturday 19th September 1987. The two groups set off on the same train, but return separately. The groups are:

- a) The Americans. A group of 12 adults from the USA which is at present touring Britain. The Americans plan to spend the nights of 18th and 19th September at the White Lion, Haworth, near Keighley. Some of the group wish to spend the Saturday in Haworth; others want to go for a day trip to Carlisle. You are to be the guide on the Carlisle trip. (See task A.)
- b) The 'Over 70's'. You have promised to organise a day out for a group of them which will include both train and bus travel. They can't walk far and the cost must be kept down. (See task B.)

#### a) The Americans

It is the evening of Friday 18th September, the day before the trips. You go to the White Lion in Haworth to answer questions from the Americans about their trip to Carlisle.

1. Using the information sheets, write down answers to their questions on a copy of the table shown below. (Their first three answers have already been given.)

How will we go to Carlisle?	By train from Keighley station.
How do we get from Haworth to Keighley?	By bus; it only takes 15 minutes or so.
When does the train leave Keighley station?	At 9.05 a.m.
When does it get to Carlisle?	
We want to be back at the White Lion by 7.30 p.m. When do we have to leave Carlisle?	
How long will we have there?	
How much is the train fare?	
Roughly how long does each train journey take?	
What is there to see in Carlisle?	5
Tell us some interesting sights to watch out for from the train.	

Page 1

M41

#### PAPER 2

#### Trips on the Leeds – Settle – Carlisle railway (continued)

#### a) The Americans (continued)

- 2. You plan to take the Americans on a sight-seeing walk around Carlisle. A map of Carlisle and a plan for the walk are shown on page 3 (M43). Read through the plan carefully, and, on a copy of the map, show
  - a) the *route* of the walk
  - b) the likely positions of the underlined landmarks, using the letters given in brackets. (For example, the <u>Citadel</u> is at 'A'.)
- 3. Estimate the total length of the walk in metres.
- 4. Some of the party want to spend 20 minutes in the Lanes Shopping Centre. What is the latest time that the group should be walking past the Civic Centre, if they are to be sure of catching the train without hurrying?
- 5. As you pass the Civic Centre, a lorry driver stops to ask you how to get to the Victoria viaduct. Write down clear directions for a route for the driver.

#### b) The 'Over 70's'

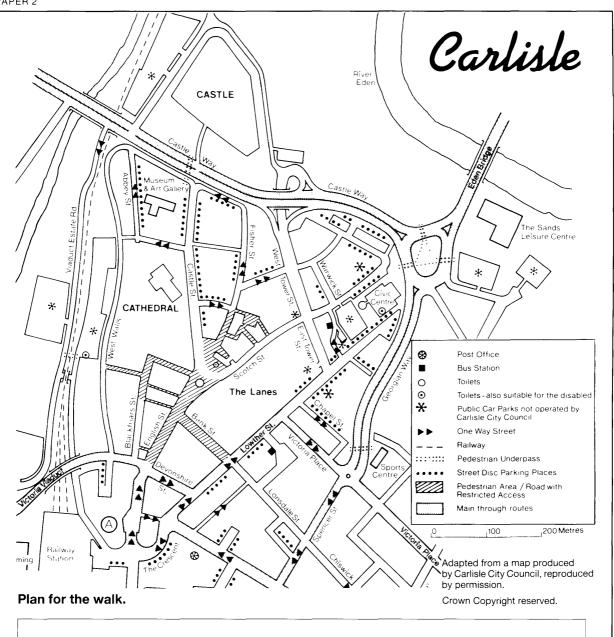
You visit the 'Over 70's' club to plan their day out for them. First you find out what they want . . .

'We don't want to spend more than £7.00 each on travel.' 'We'd like to go on the train and on a bus – see some nice scenery – have a cup of tea somewhere interesting – buy some souvenirs for folks at home.' 'We don't want to be back too late.'

- You recommend that they travel by train to Garsdale and then by bus to Sedburgh or Hawes. You have already found out that the bus fare from Garsdale to Sedburgh costs £1.00 return, and the fare from Garsdale to Hawes costs £1.10 return. Give as many details as you can of each of the two alternative trips, so that the club members can decide which they prefer.
- 2. They ask you which of the choices in question 1 you think is the best. Say which you would recommend it.
- 3. Assume that they agree with your choice, but would like some further information. Answer their questions.
  - 'How much will the travel cost each of us?'
  - 'How long will we have there before we catch the bus back?'
  - 'I have a friend in York who wants to come. How much would the travel cost her? What is the earliest time she could get back to York?'

Page 2





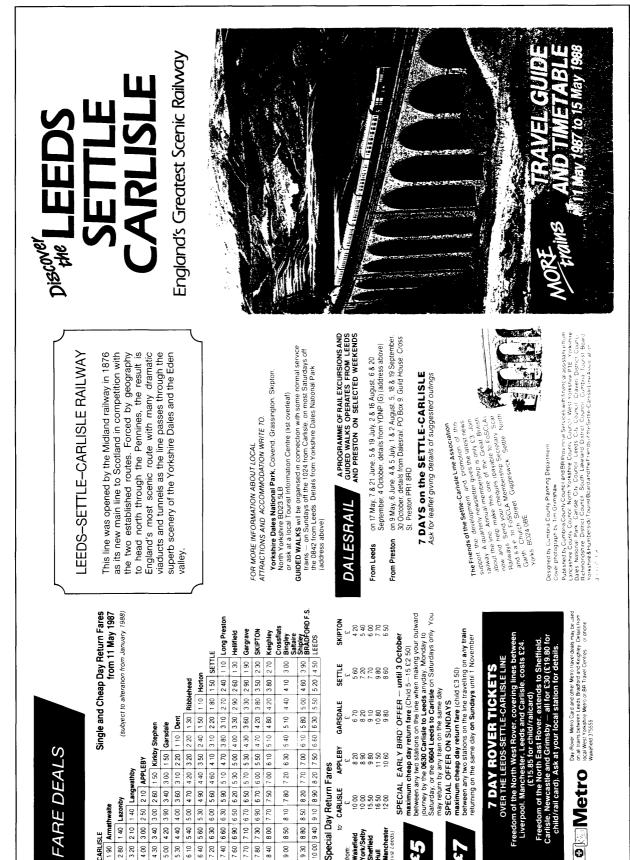
After arriving by train, walk past the <u>Citadel</u> (A), then turn left at the crossing, along Victoria Viaduct. Look for the little street, second right, called <u>West Walls</u> (B). Walk along West Walls a little, then turn first right along St Cuthbert's Lane, with <u>St Cuthbert's church</u> (C) on the left, just after Blackfriars Street, and so into the Market Square, with the <u>Market cross</u> (D) facing you. Turn to the left and you'll see the old <u>Town Hall</u> (E). Walk along Castle Street a little, then left into the Cathedral grounds, opposite the one-way street. After looking at the cathedral, continue past the black gates into <u>Abbey Street</u> (F) with the museum at the right.

Leave the museum by the rear exit, then under the <u>archway</u> (G) into Castle Street and through the subway to the Castle grounds. You can picnic or walk along the River Eden in nearby <u>Bitts</u> <u>Park</u> (H). Return to the station through the roundabout underpass, passing the Civic Centre on your left. Turn right opposite the car park, then left, and over the crossroads into <u>Market Street</u> (I). Turn left and you are soon back in the Market Square.

You can browse around The Lanes shopping centre before returning to the Railway Station.

Page 3

M43



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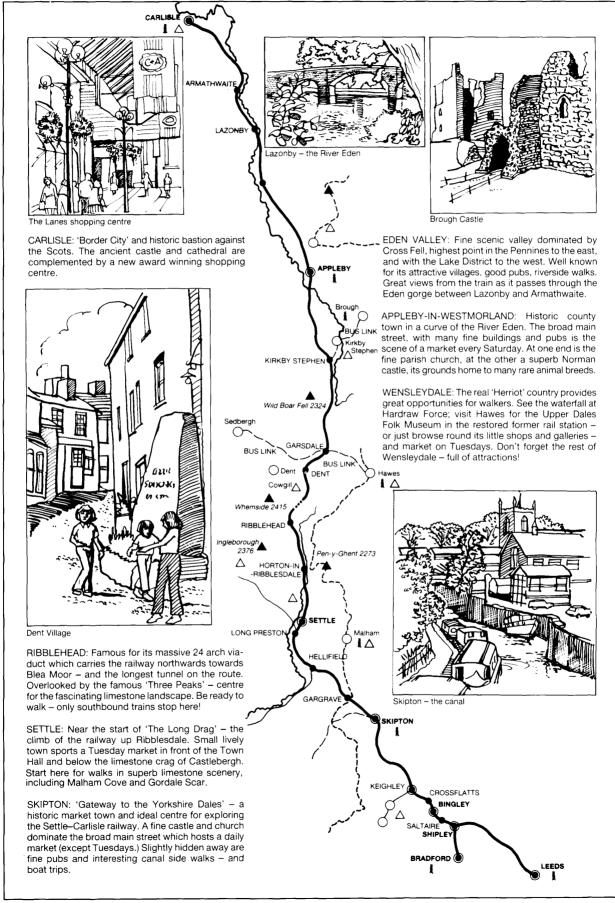
#### PAPER 2 INFORMATION SHEET

M45

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#### PAPER 2 INFORMATION SHEET



# What do the students and teachers think?

While preparing this module we obtained the views of students in a few of the trial classes by tape recording interviews with small groups.

The following interview took place while a class of 'low ability' 4th year secondary students was working on Stage 3 of the module. Four students (S1, 2, 3, 4) were interviewed; each was chosen from a different group in the class. The interviewer was not the class teacher but a 'friendly, interested but uninformed observer'.

- I: So where are you all going?
- S1: Skegness.
- I: What have you done so far?
- S1: Made a big list out, seeing what jobs we've got to do; then we tick which ones we've done so we know if we've missed out any . . . we've got to phone the coaches up. Then there's the trains.
- S3: There's a problem. We need to get a train that leaves early in the morning and one that leaves at a reasonable time in the afternoon, but yesterday they said the earlier trains were too late for us, I've go to check that now.
- S3: The first time we had to phone, I said 'I'm not phoning, I'm not phoning!' but half way through you get used to it, kind of thing, so when you leave school and you want to phone up for a job say, you don't feel so bashful.
- S2: It gives you more confidence.
- S1: Yes.
- I: Would you think of doing something like this . . . planning a trip yourselves in the holidays.
- S2: Yes, there's two people in our year planning to go youth hostelling.
- S1: But if we went it wouldn't be planned like this. We'd just go!
  - I: Is it worth planning, then?
- S1: Yes because if you don't you're bound to forget something!
- S3: It's more organised. (S4 runs into the classroom.)
- I: What's happened now?
- S4: We've just been phoning up coach companies and the cheapest was £100. We've found one for £90 for a 20-seater. We've rung round quite a few. Some are too expensive. Some are not there anymore. Gone bust or something!
  - I: Would that be worth considering . . . the £90 coach?
- S4: We'll need a calculator!
- S1: There's two maths groups . . . some may come from the other class . . .

Notice the involvement, autonomy, growth in confidence and the natural way in which mathematical activity is beginning to arise.

The following unsolicited letter vividly illustrates the tensions that many teachers feel as they attempt to encourage such student autonomy through real problem solving.

'I found it very difficult not to intervene and direct work to begin with. It took me a while to realise what I intended as open-ended suggestions like 'Have you thought of trying

. . . ?' were simply interpreted by the students as 'Do this!' It was difficult to stand back and allow them to make mistakes or explore blind alleys.

I found I had to simply grit my teeth and survive the noise, arguments and apparent chaos of the first few lessons but gradually we all became much more relaxed and involved in the activities, and things settled down considerably.

The students initially complained that we were not doing 'proper maths' but as they became more involved in the modules and discovered they enjoyed doing the work, the complaints became less frequent. Now after four modules I think they are beginning to see that in fact they have developed some very valuable skills through the work and that it may be of more use to them than 'proper maths'.

Using the Numeracy Project has had a significant impact upon my relationship with the class. I feel I know the students much better than I have ever done in an equivalent class and that in many ways they relate to me much more as a friend than as a teacher. I am sure this is because they have taken responsibility for their own learning and have had to make and live with decisions which have affected the whole class. I have certainly discovered talents and personal qualities in many of them which would never be revealed in a traditional maths classroom. A below average maths class has been transformed into a very impressive and interesting group of young people - or perhaps they always were?

Finally, if you have any views or experiences on your work with this module, we do hope you will let us know.

# **Checklist for the teacher**

Real problem solving demands a different balance of teaching styles and strategies from the traditional curriculum. Students need to learn how to

- assume more control of, and responsibility, for their work
- share and develop ideas with each other
- give and accept constructive criticism
- turn their own ideas into actions, and to learn from the consequences of their own decisions.

To effect this change of roles, it is helpful if the teacher can:

#### Frequently Those seem to be really good ideas. praise achievement Can your trip cater for people who don't like sport? encourage groups to think further and deeper Can you explain that to me again? I didn't quite understand. ask clarifying questions Do you think you could finish your agree targets rough plan by Monday? Tell me what you'll say on the encourage students who lack phone . . . Good, I'm sure you'll be O.K. confidence. Occasionally make a suggestion if a group is Why don't you visit the running out of ideas tourist information office after school? divert a group from a particularly Do you have to spend that much unhelpful idea on transport? Avoid taking over a problem I'll phone the station for you if you like. making negative comments You're being much too ambitious. determining whose view is Sarinda's idea seems to be the best. accepted.